

Soil Liquefaction

地盤の液状化

Damage Caused by Earthquakes

- Human damage was caused by tsunami, collapse of structures, and fire.
- Damage to infrastructures, such as roads, bridges, **harbor facilities** is often related to liquefaction.
 - In 1995 Hyougoken-nambu Earthquake infrastructures were severely damaged by liquefaction.

Liquefaction as a Disaster

- Liquefaction has been recorded as a natural phenomenon from ancient age.
- Liquefaction was widely recognized as a natural disaster after two earthquakes in 1964.
 - ***Niigata Earthquake*** (Japan)
 - ***Alaska Earthquake*** (US)modern structures were severely damaged.
- Research activities on liquefaction have been led by the US and Japan, since 1964.

Evidences of liquefactions in ancient age



Archaeological excavations reveal the evidences of liquefaction (sand boiling) .

Research Activity on Liquefaction in Japan

- **Mechanisms of liquefaction**

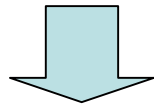
- Element test and model test

- **Classification of damage**

- Site investigation of the damages

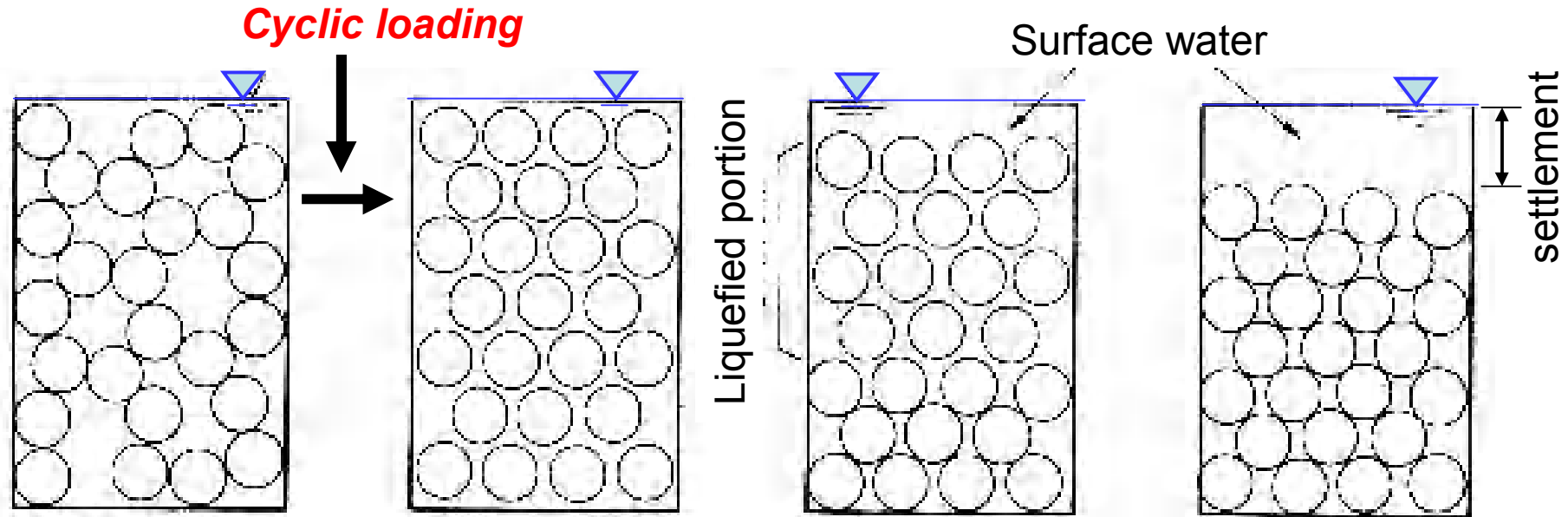
- **Evaluation of liquefaction potential**

- Site exploration and laboratory test



Earthquake resistance design + Counter measures

Process of liquefaction from onset to termination



(a) Before liquefaction,
Loosely
 saturated
 sand deposition

(b) Just after
liquefaction.
 All particles are
 suspended in
 water.

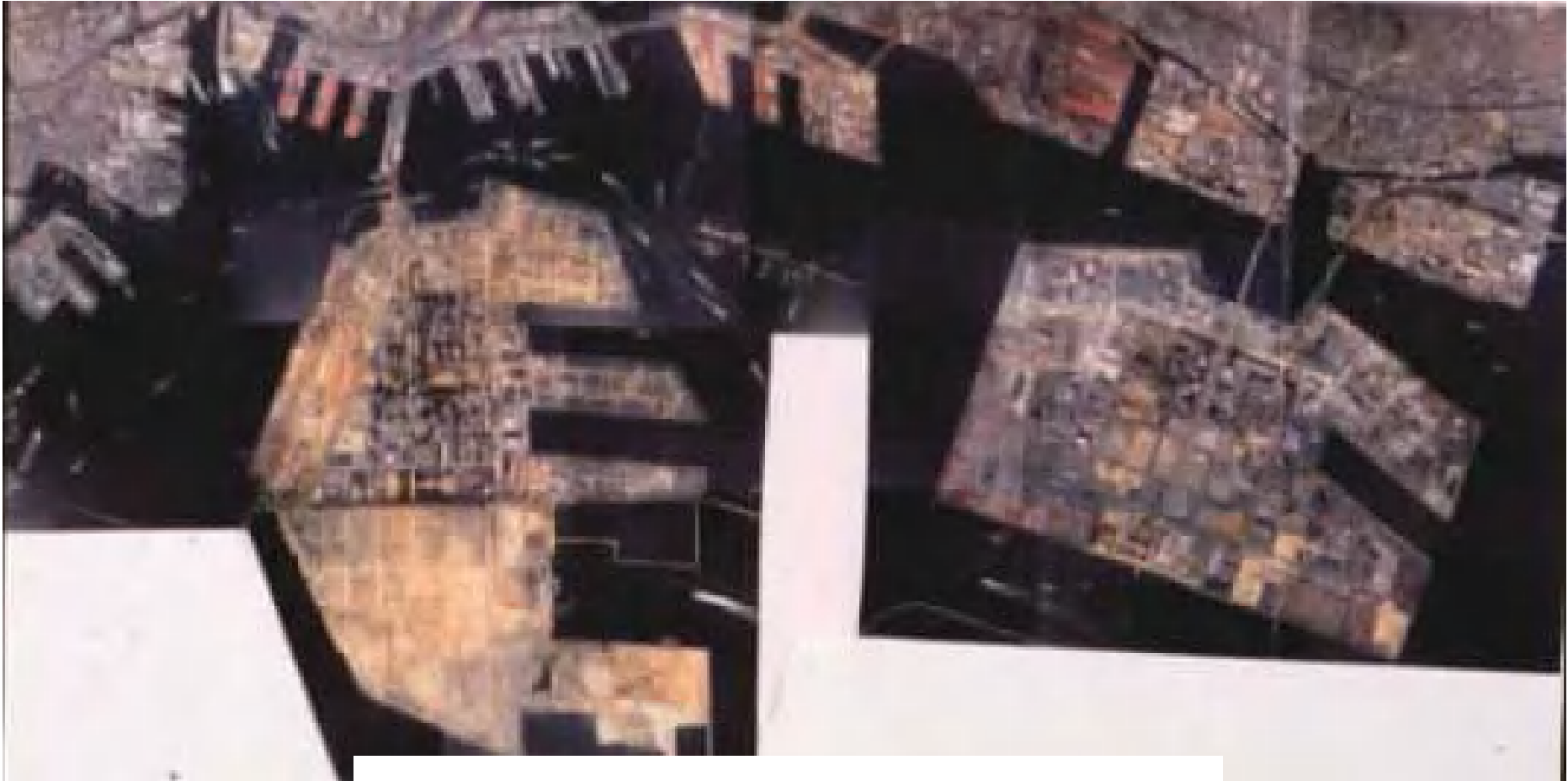
liquefied

(c) After a certain time
 At the bottom,
 liquefaction is
 terminated, but not
 at the top.

(d) After long time
 No liquefied portion.
 Densification of
 sand causes
 settlement.

volume decrease

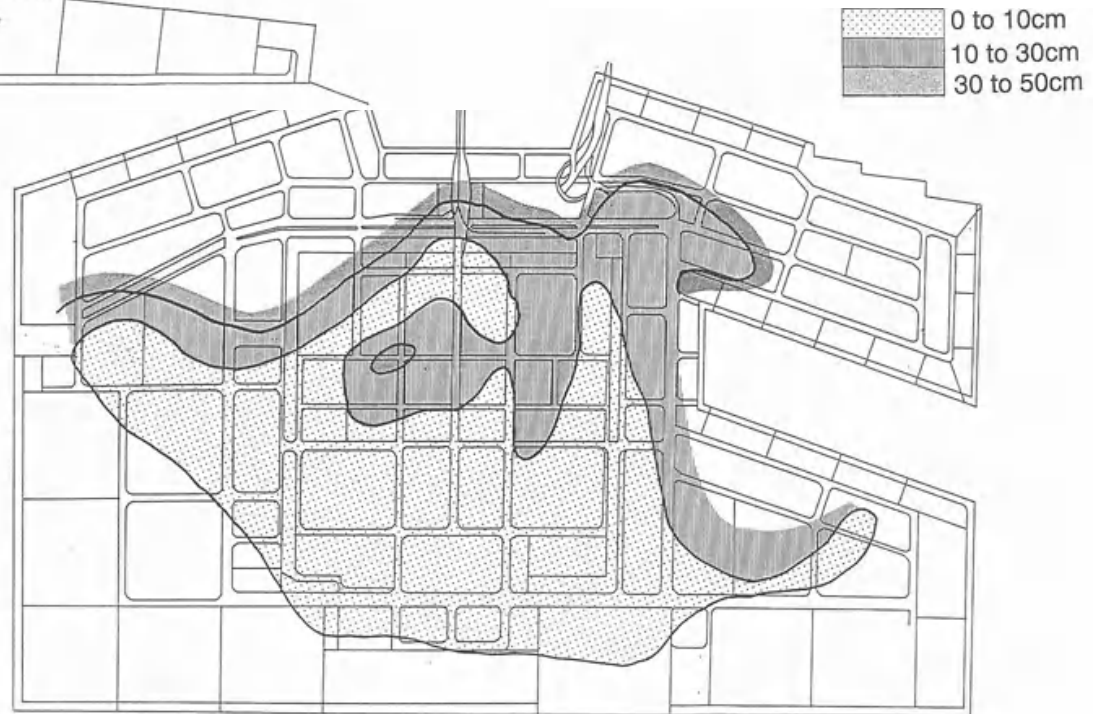
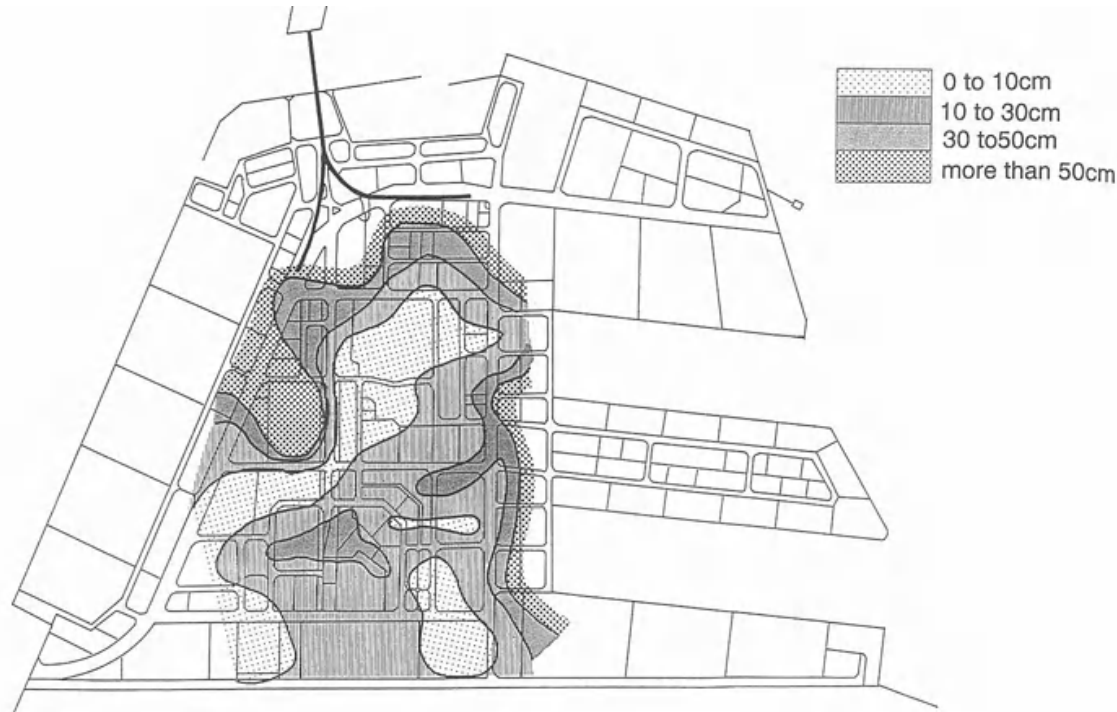
Water Front in Kobe City after 1995 Hyogoken Nambu Earthquake



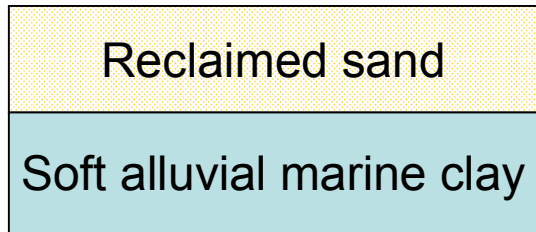
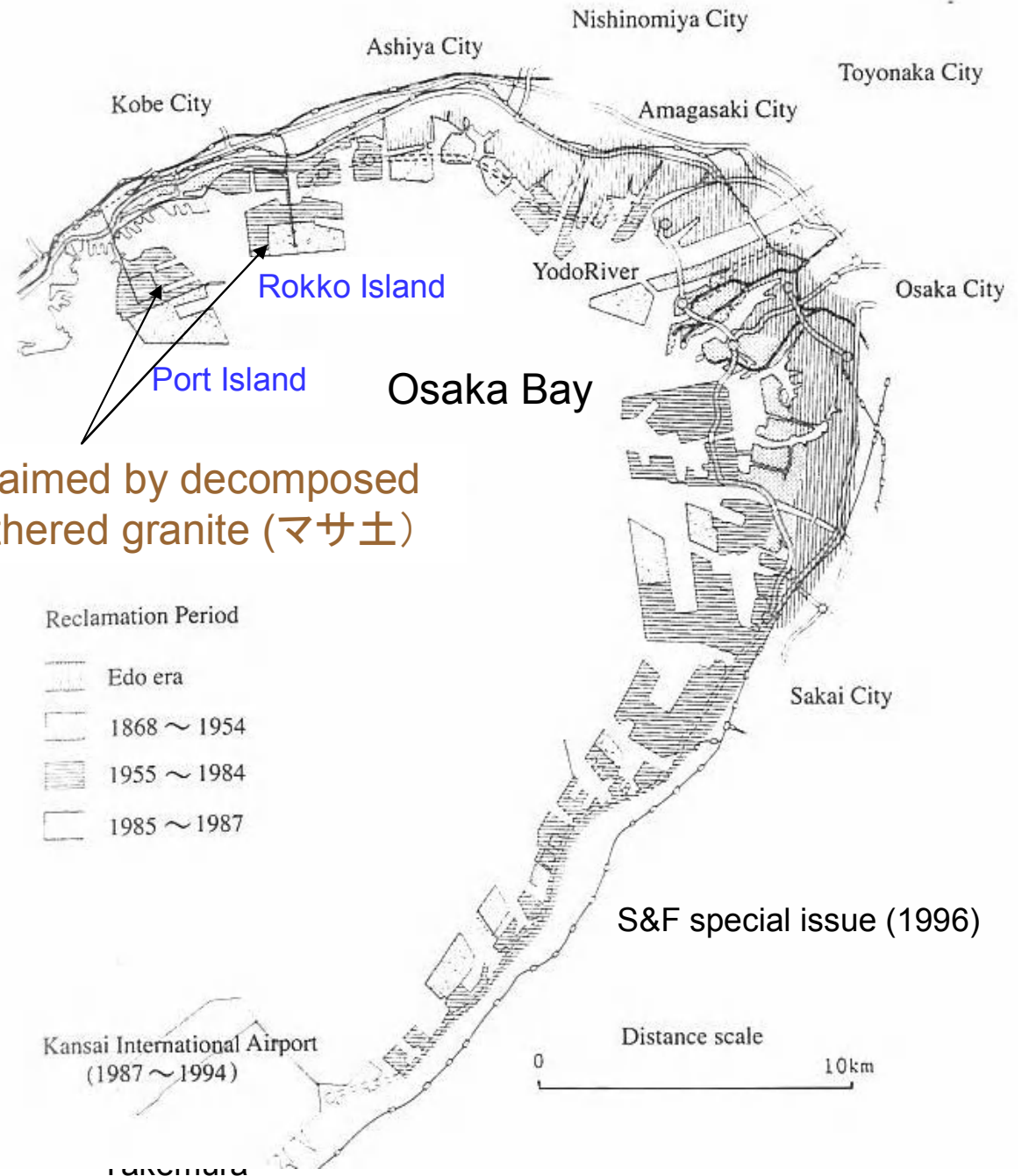
liquefaction occurred extensively

Settlements at reclaimed islands observed at 1995 Hogoken-Nanbu Eq.

S&F special issue (1996)

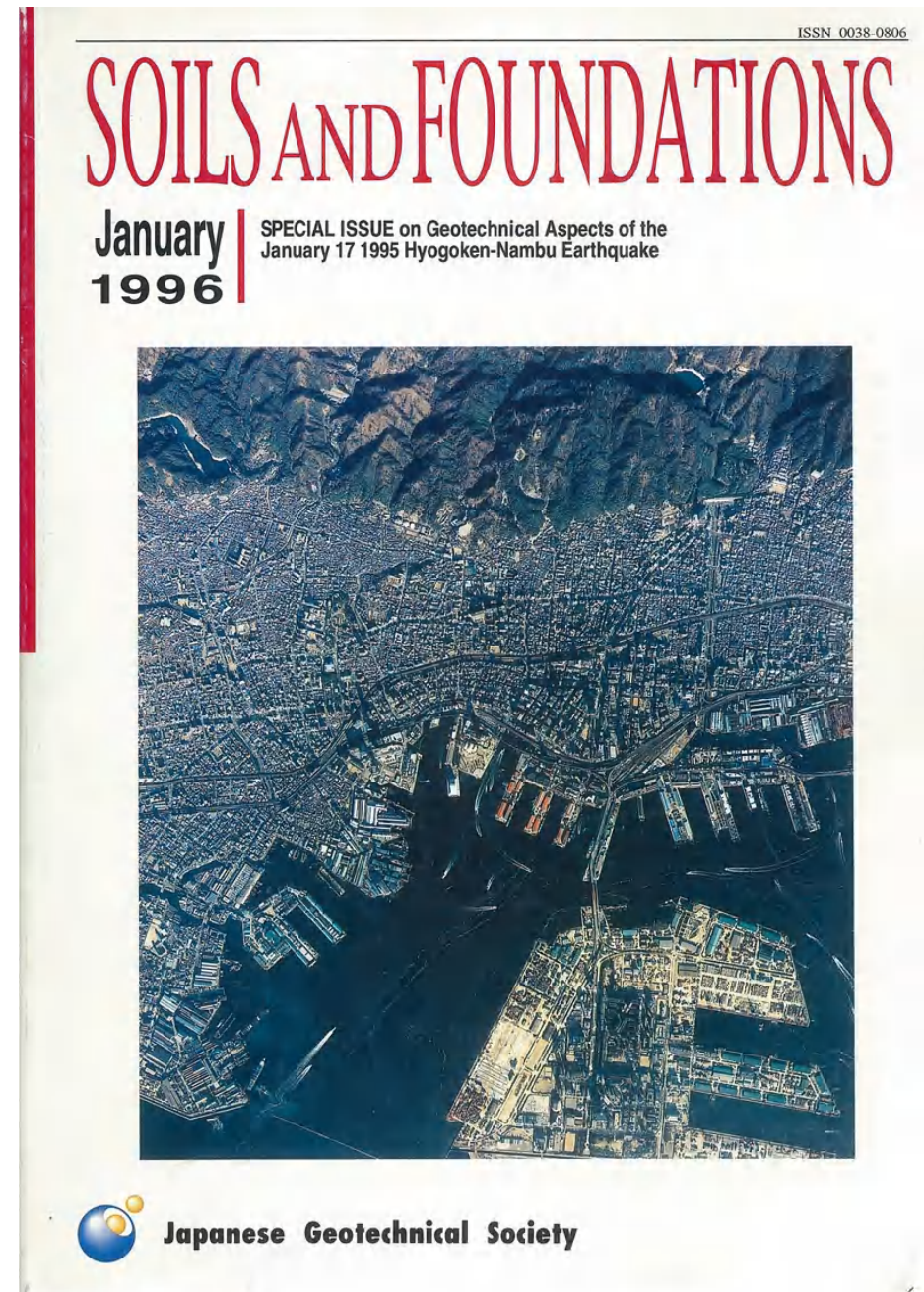


Reclaimed lands in Osaka Bay



Typical soil profile of reclaimed land in Osaka Bay

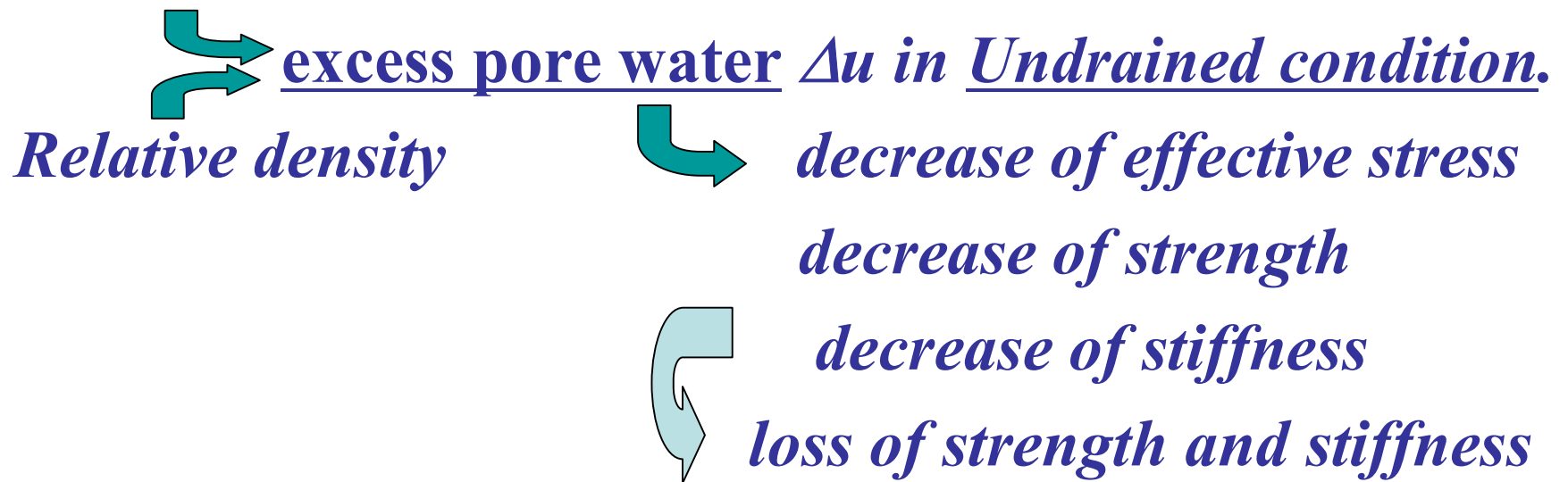
Soils & Foundations
Special Issue
January 17 1995
Hyogoken-Nanbu Earthquake



Mechanism of Liquefaction

- Liquefaction mechanism in sand element
 - Rearrangement of sand particles
 - Motion of sand particles under water
 - **Volume change due to shear deformation**

[**Dilatancy**] in *Drained condition*



The Principle of Effective Stress

-Basic principle in Soil Mechanics-
by Prof. Karl Terzaghi

Stress in soil: Total stress = effective stress + pore pressure

$$\sigma = \sigma' + u$$

“All measurable effects of a change of stress, such as compression, distortion and change of shear resistance, are exclusively due to change in the effective stress.”

Strength, stiffness of soils = $f(\sigma')$

ex) $s = c' + \sigma' \tan \phi'$
 $G = C \sigma'^{1/2}$

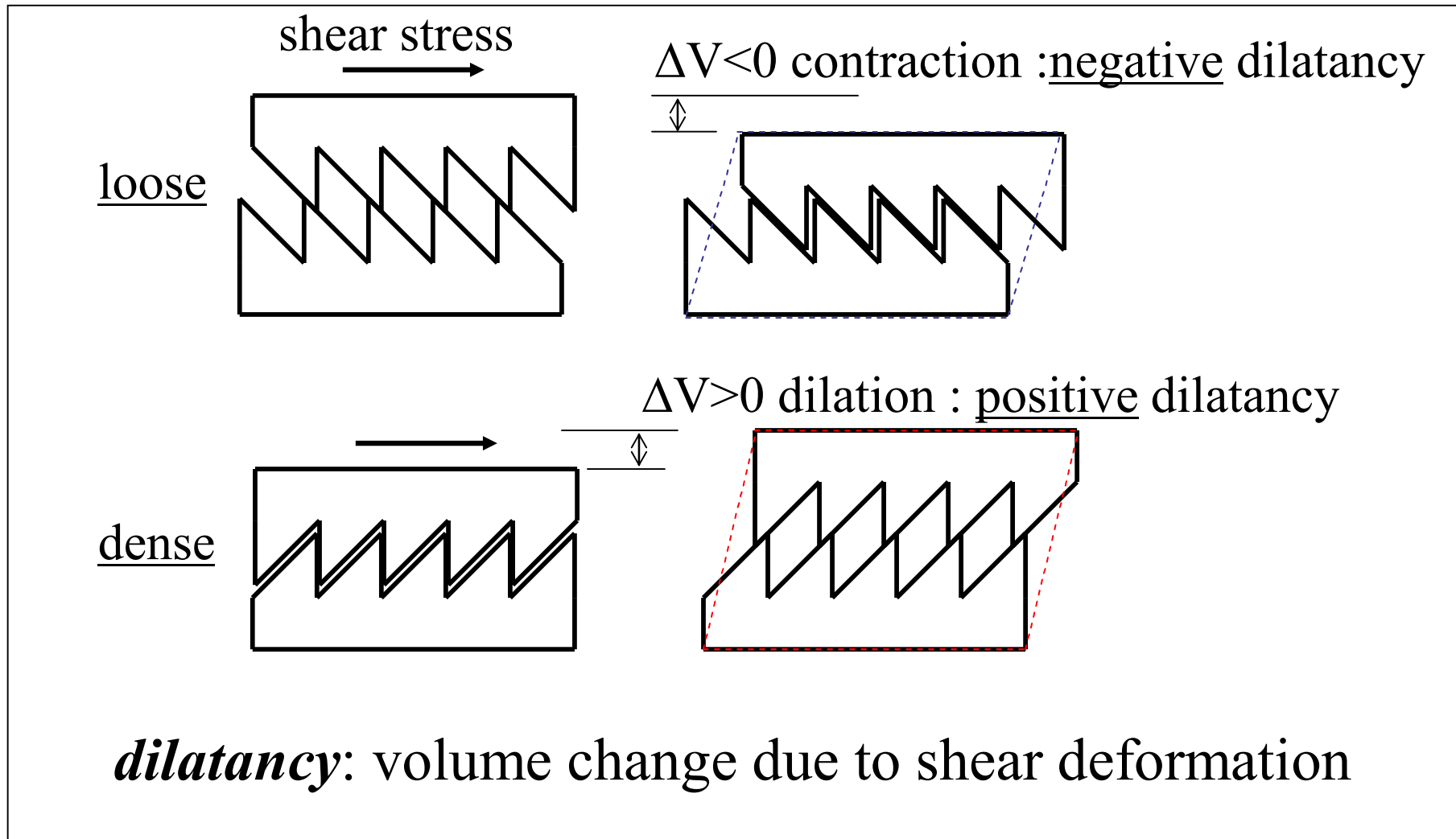
if $c' = 0$ and σ' is 0, $s = 0$ and $G = 0$.

increasing u \Rightarrow decreasing s and G .

$u = \sigma$

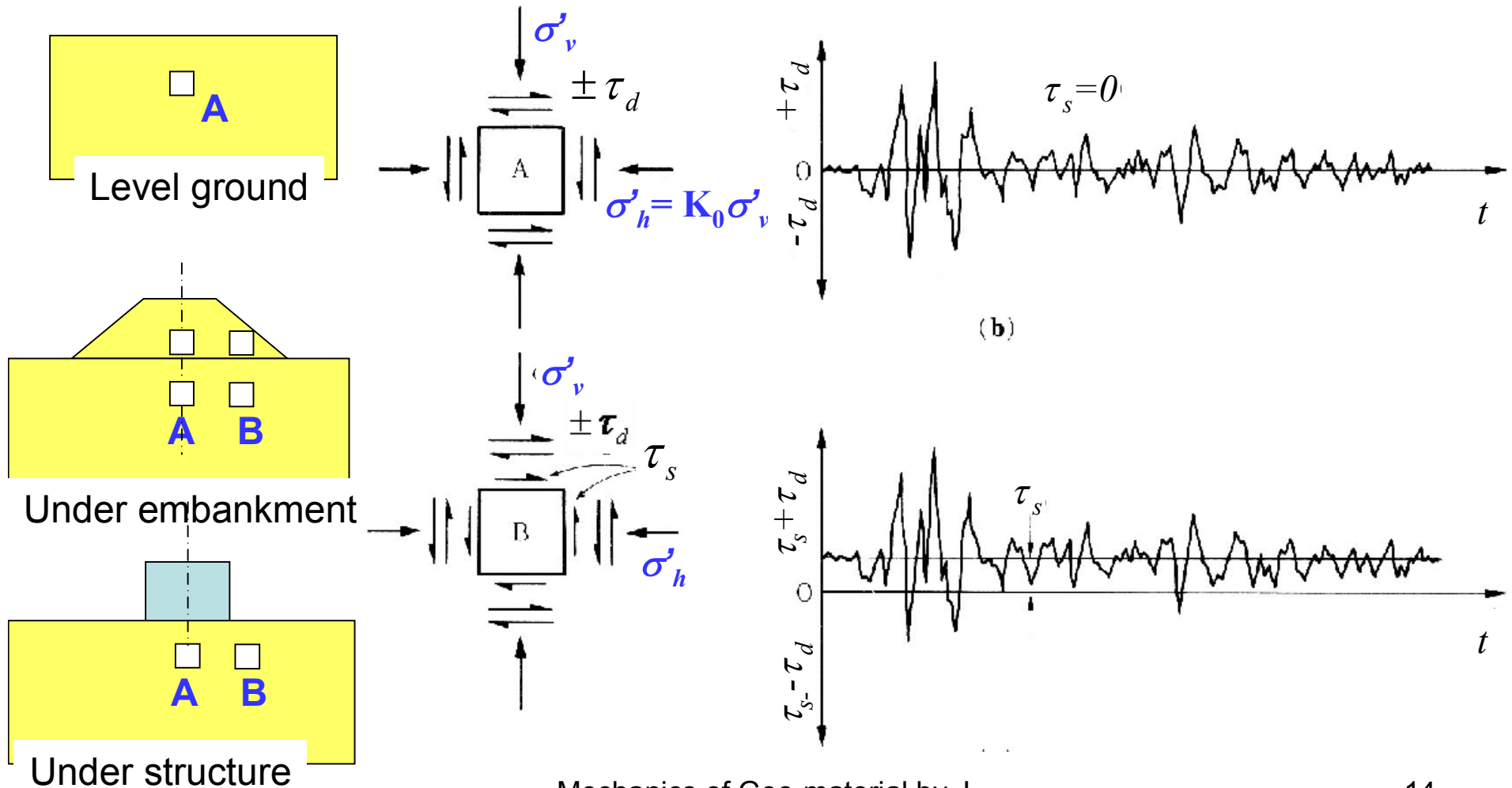
liquefaction \curvearrowright

Analogy of dilatancy of granular material



Static and dynamic shear stresses in soil elements during earthquake

Initial stresses

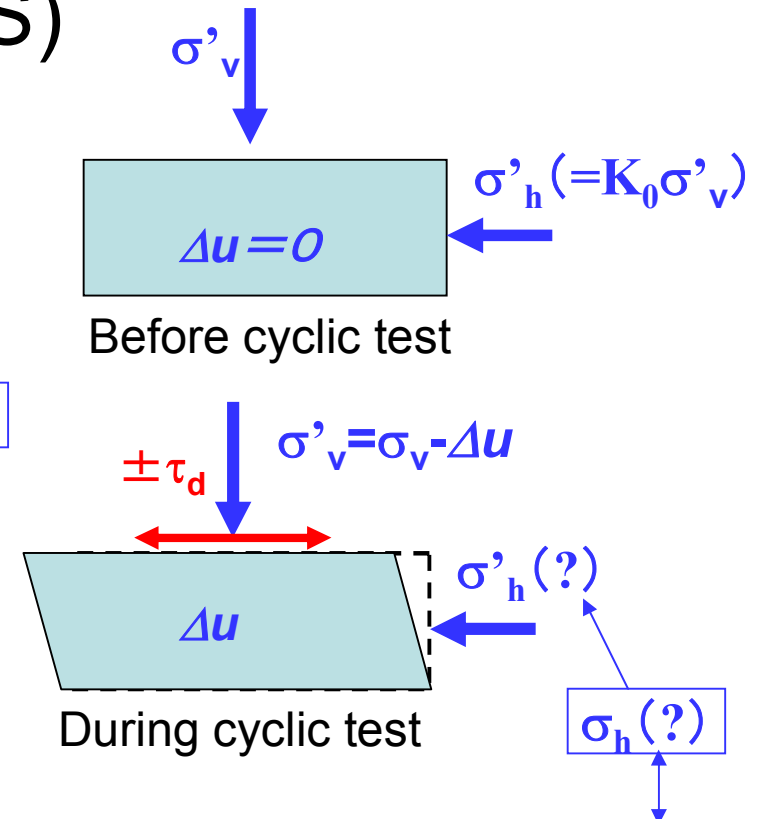
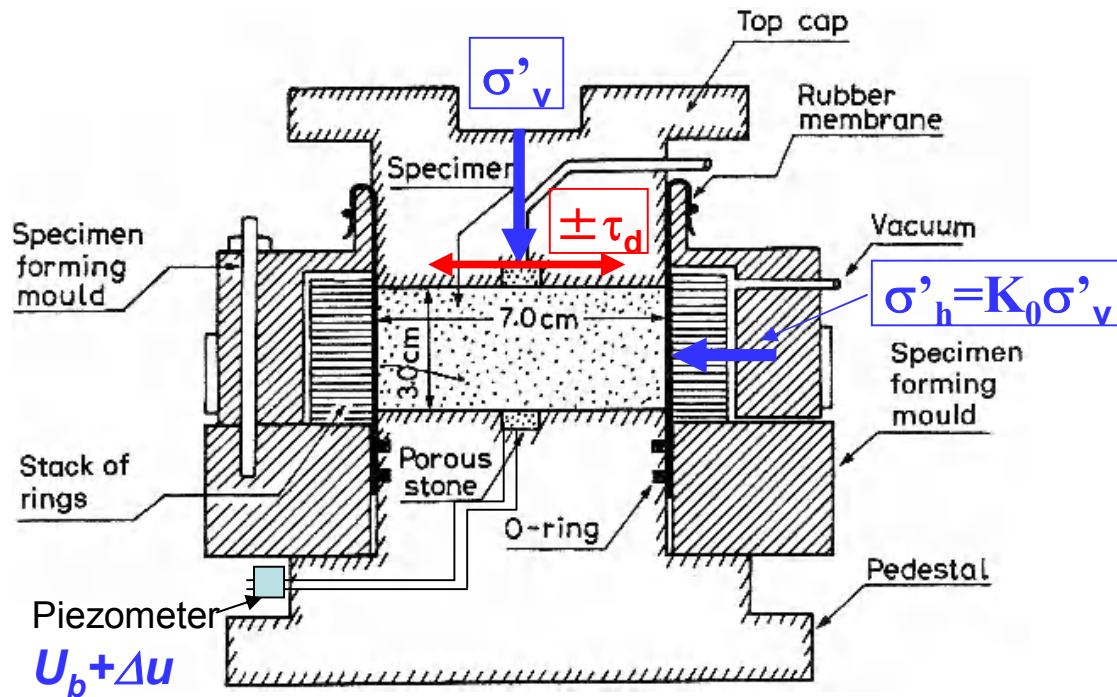


Element tests on liquefaction

Cyclic shearing tests:

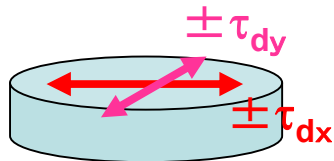
- **Triaxial test(三軸せん断)** (commonly used for design);
- **Direct simple shear test(直接単純せん断)**
(mainly for research);
simulating real stress conditions, (initial, cyclic shear by EQ)
 K_0 consolidated sample, simple shear
- **Hollow cylindrical torsion test(中空円筒ねじりせん断)**
(mainly for research)
simple shear, stress path by stress invariants
(応力不変量)

Direct simple shear test (DSS)

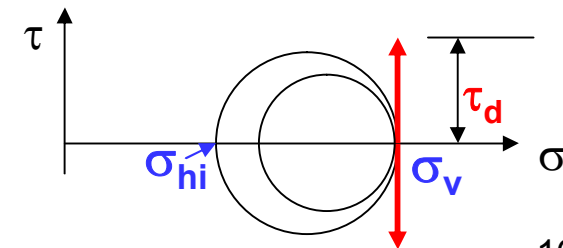


similar to real site:
because σ_h is indeterminate

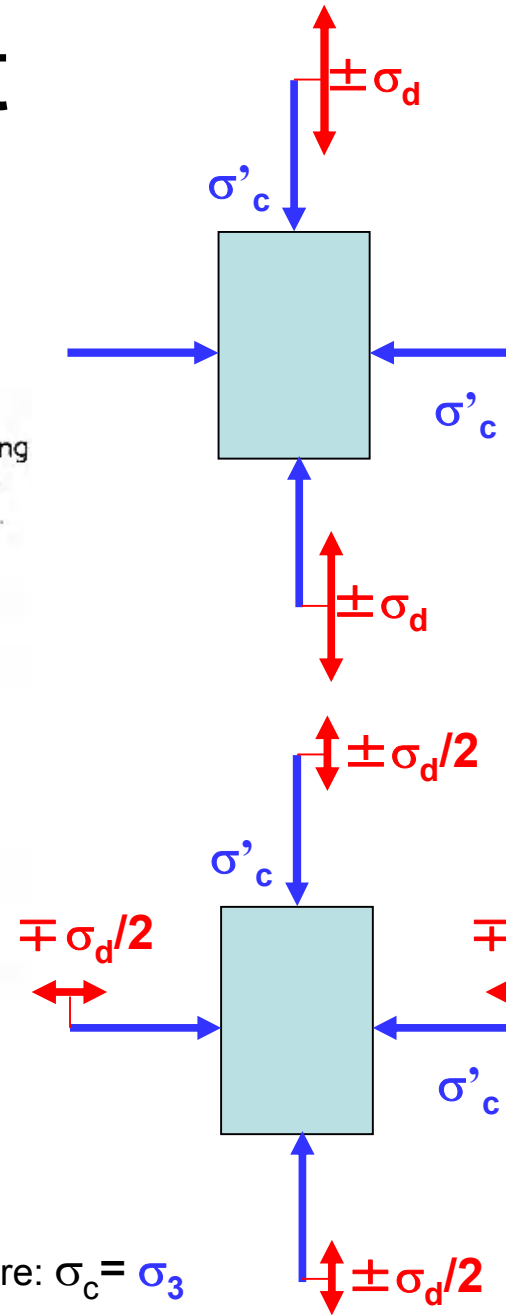
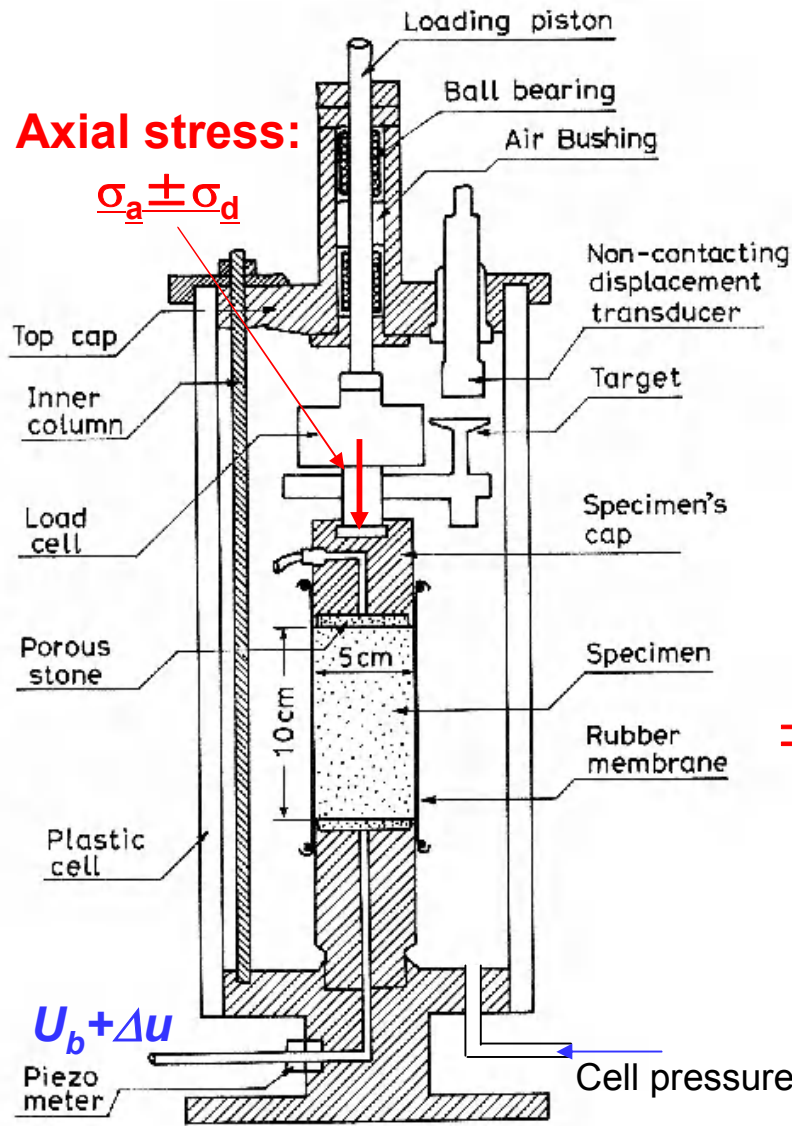
Shear stress can be applied not only in one direction but also two direction.



Total stress path on the horizontal plane.



Triaxial test



Loading pattern 1
(commonly used)

Amplitude of deviator stress: $\pm \sigma_d$

Under undrained C. with the same initial C., the **effective stress path** are the same in pattern 1 & 2.

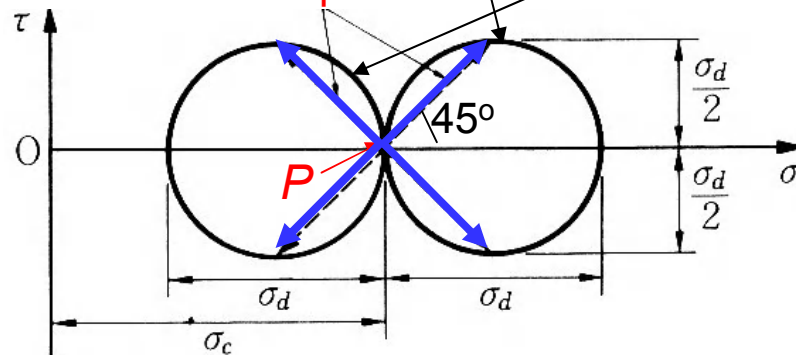
Loading pattern 2

Amplitude of deviator stress: $\pm \sigma_d$

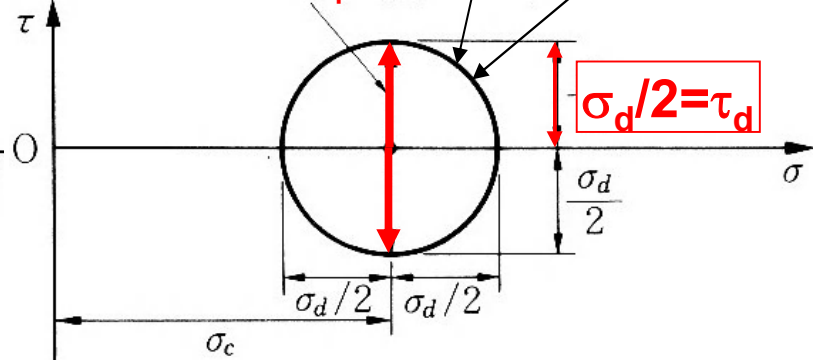
Stress path in compression and extension test

	Initial cond.	$+\sigma_d$	$-\sigma_d$	Initial cond.	$\pm \sigma_d / 2$	$\mp \sigma_d / 2$
Stress on vertical and horizontal plane	(a)	(b)	(c)	(a')	(b')	(c')
Stress on plane with 45° angle	(d)	(e)	(f)	(d)	(e')	(f')

Total SP on 45° plane

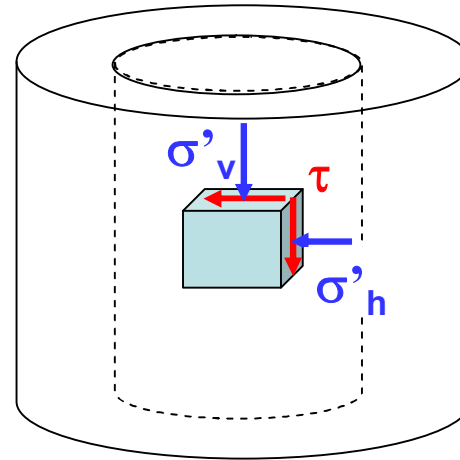
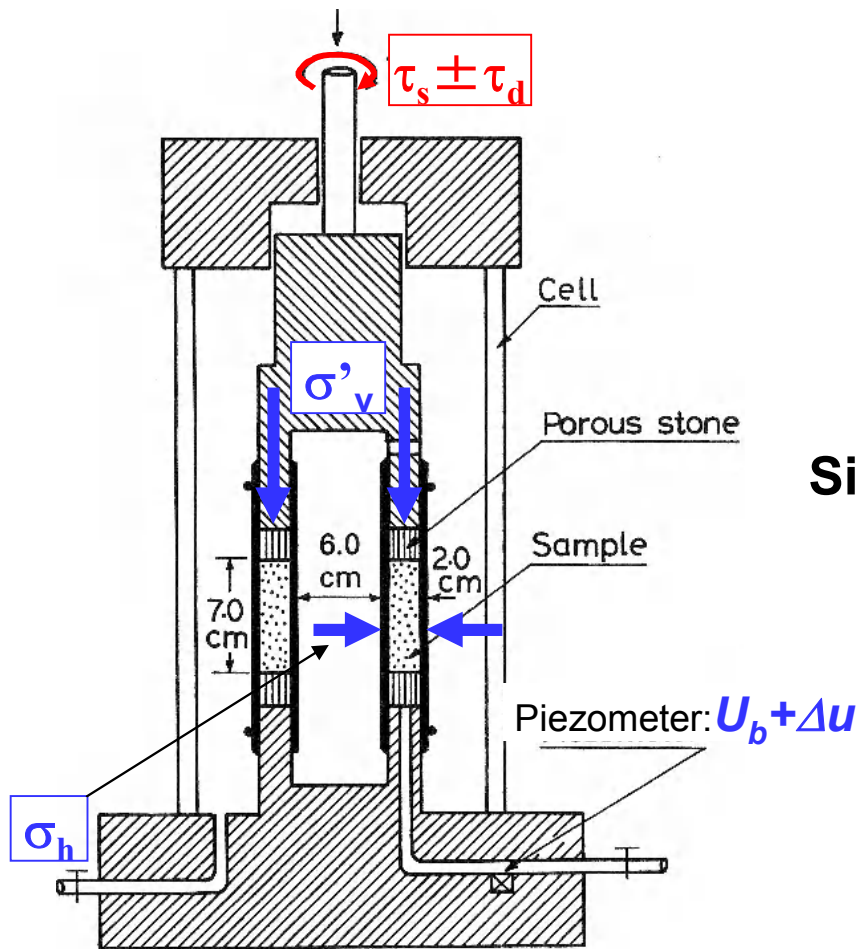


Total SP on 45° plane



Same as TSP on horizontal plane for DSS

Hollow cylindrical torsional test



Oedometer

Simple shear test:

Two types of horizontal constraint

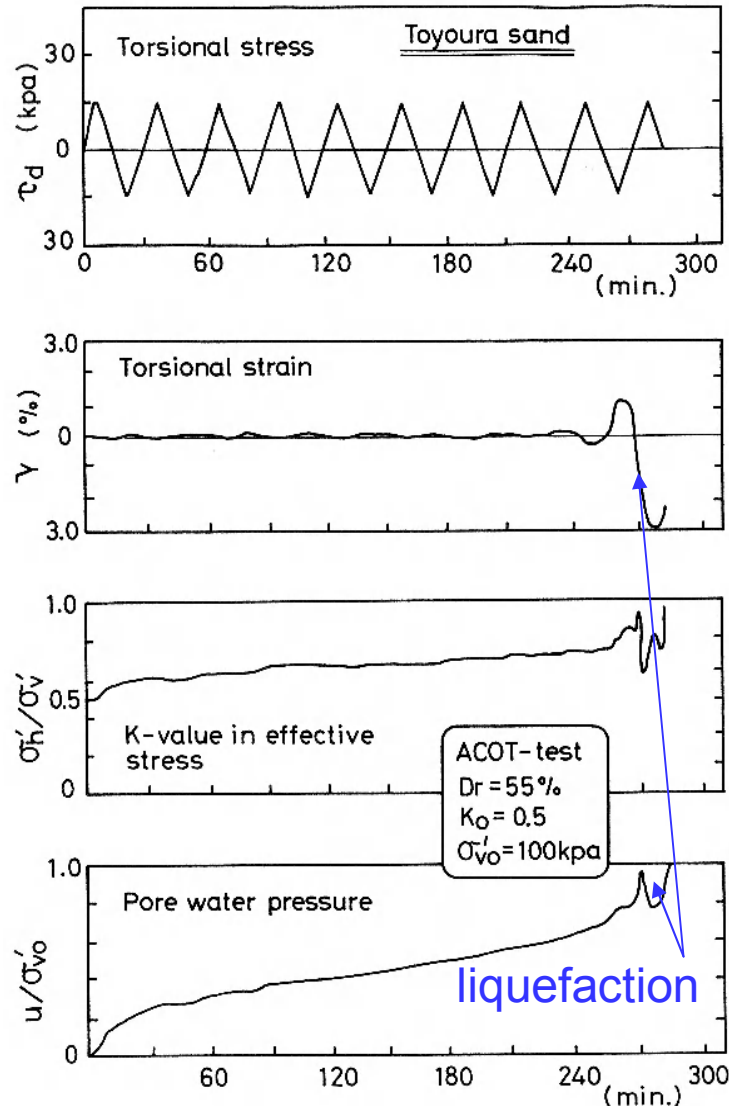
1) Horizontal strain constraint: $\epsilon_h = 0$ (DSS)
level ground

by measuring σ'_v and Δu , σ'_h/σ'_v can be observed in this test.

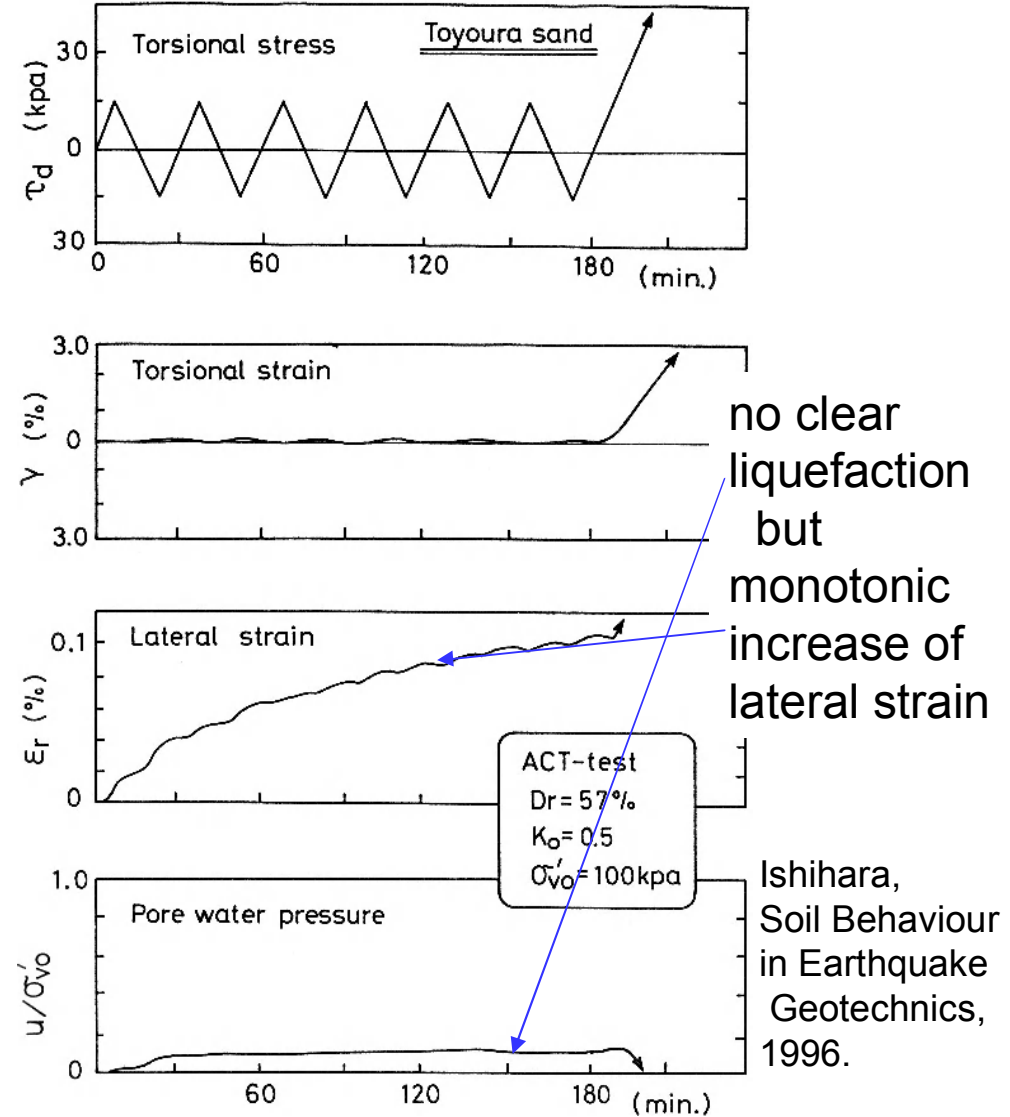
2) No horizontal constraint: e.g. $\sigma_h = \text{const}$
sloping ground (initial shear stress)

Change in lateral stress and pore pressure build-up in Hollow cylindrical torsion tests with and without lateral confinement

1) ACOT (Anisotropic Consolidation Oedometer Torsion)

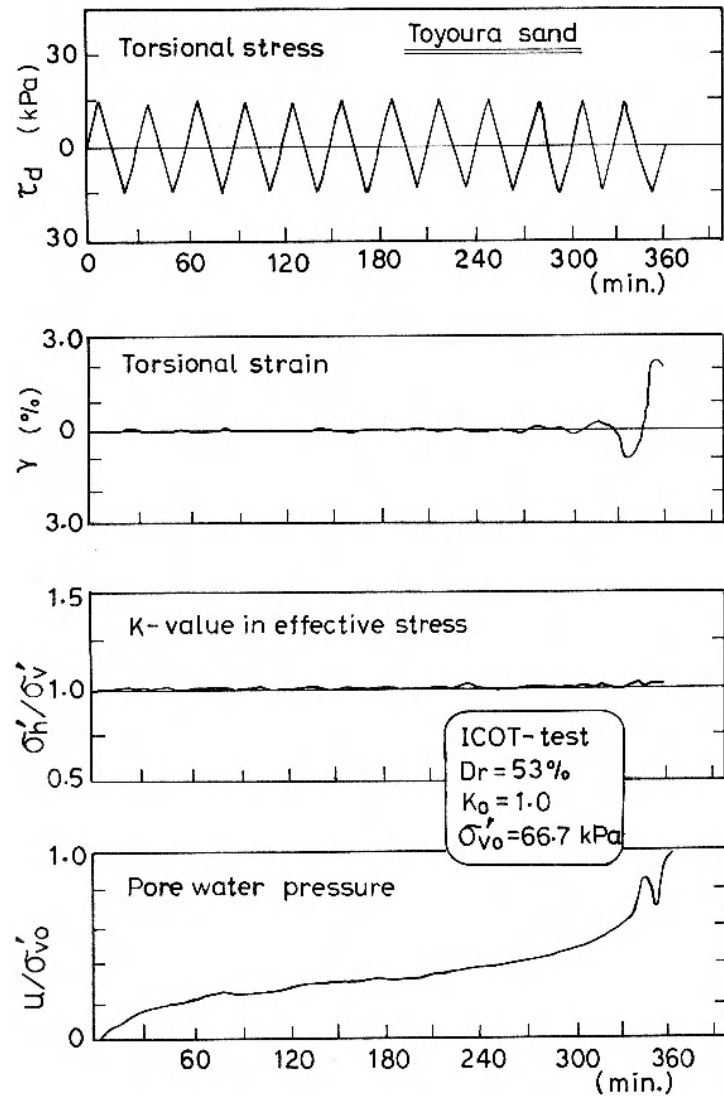


2) ACT (Anisotropic Consolidation Torsion)



Change in lateral stress and pore pressure of IC sand in HCT

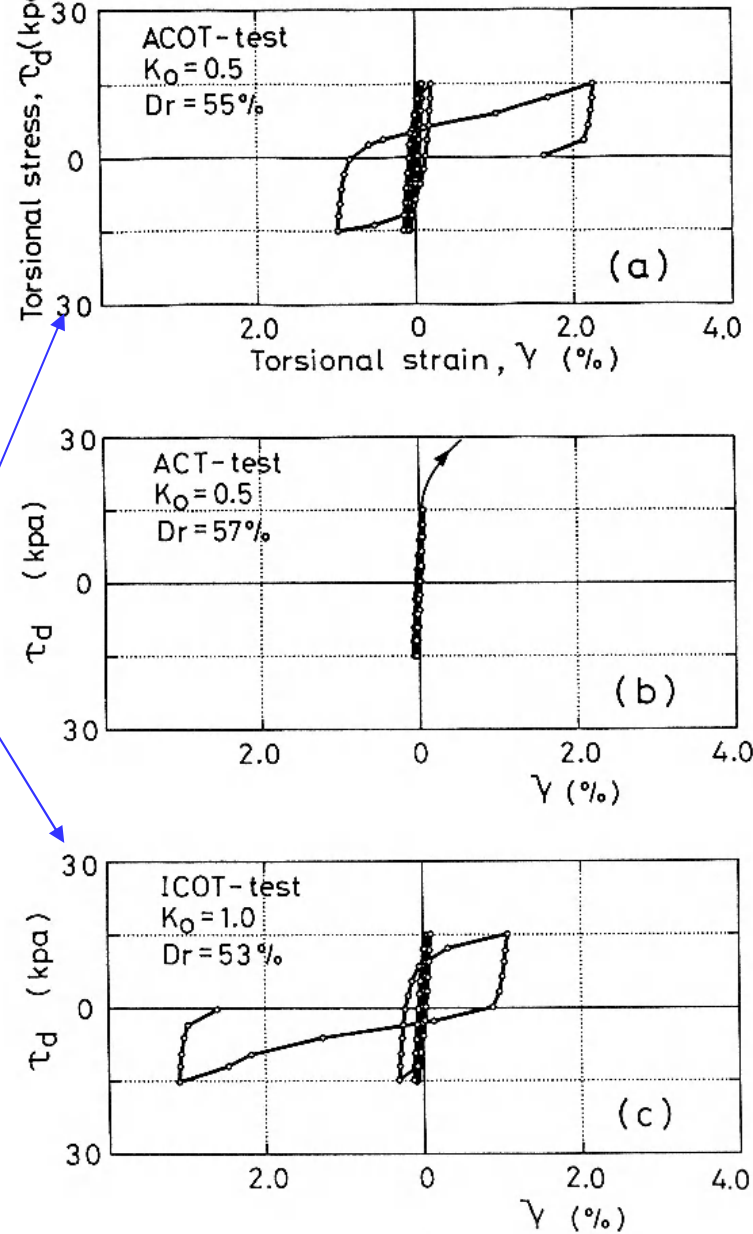
ICOT (Isotropic Consolidation Oedometer Torsion)



2007/5/10

Mechanics of Geo-material by J. Takemura

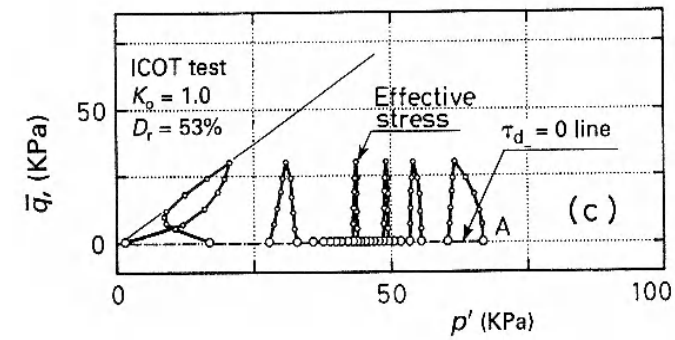
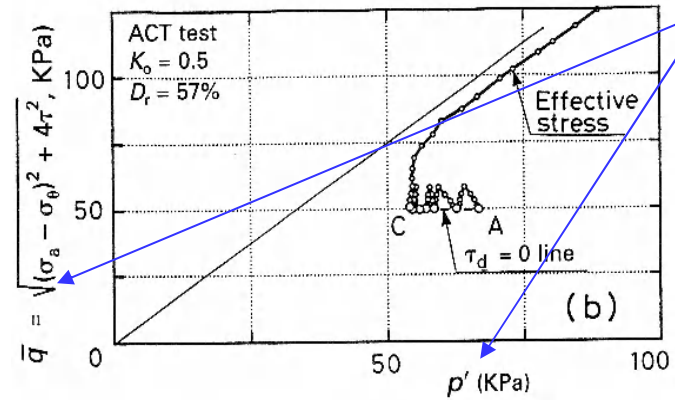
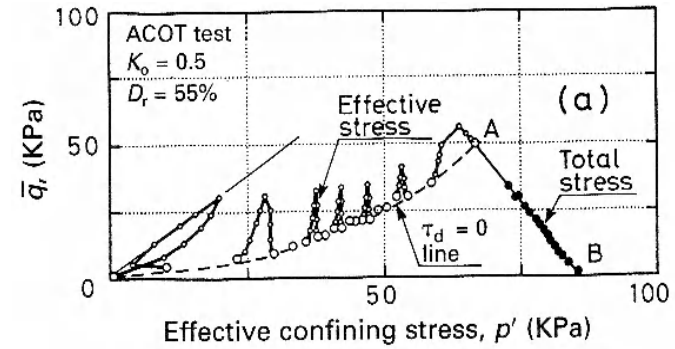
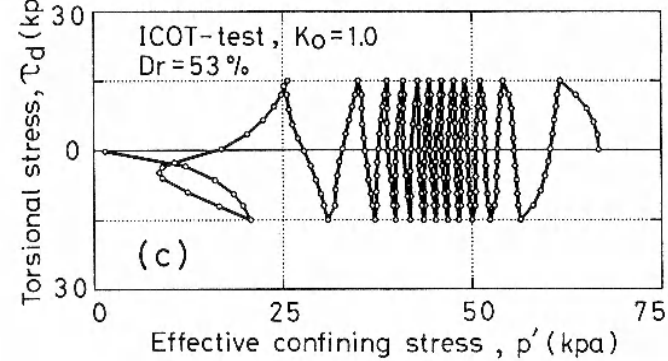
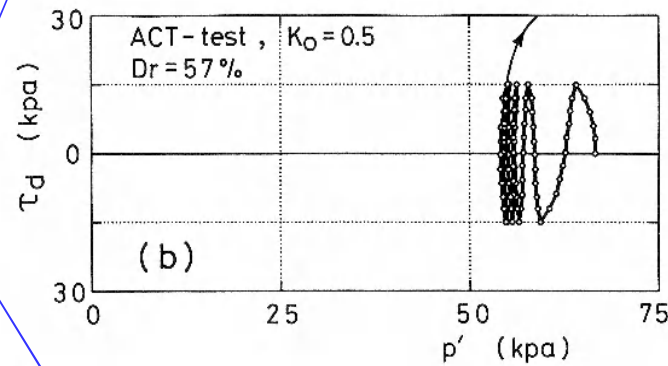
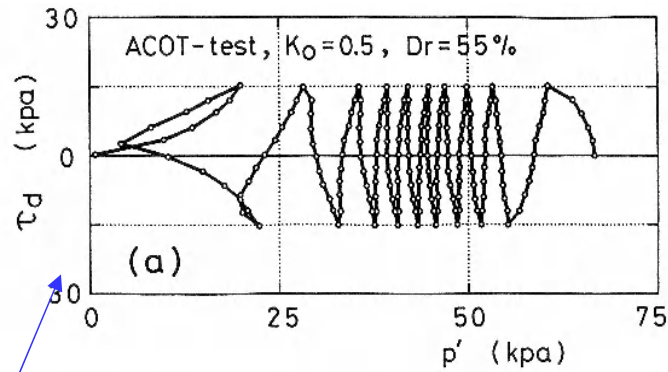
Stress-strain curves in three tests



similar

21

Effective stress paths in three types of torsion tests

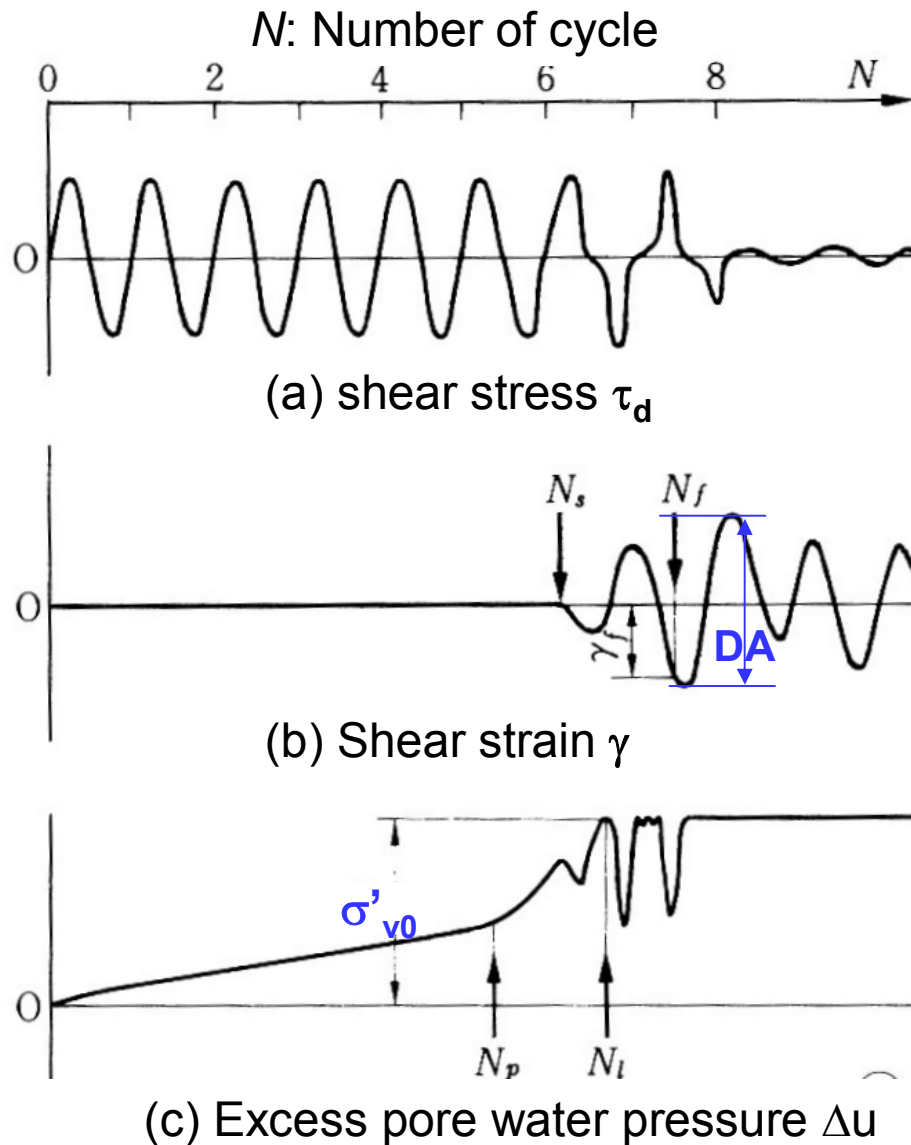


Stress invariants

Ishihara, Soil Behaviour in Earthquake Geotechnics, 1996.

similar

Behavior of loose sand subjected to cyclic loading



Definition of liquefaction points

N_p : onset of marked increase of Δu
 ($\Delta u \sim 0.5\sigma'_{v0}$);

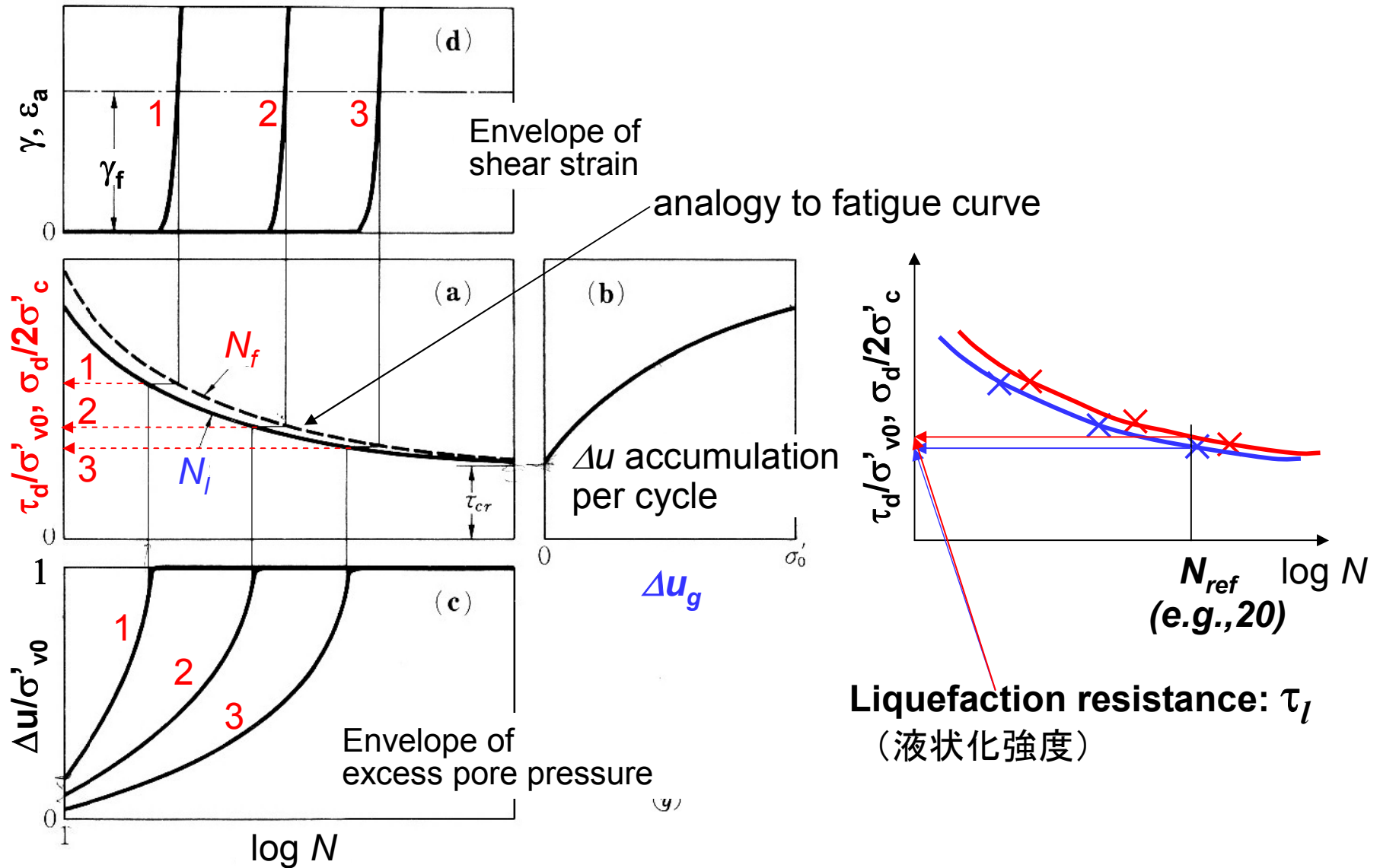
N_s : onset of visible shear strain;

N_l : Δu reaches σ'_{v0} ,
 (zero effective stress)
initial liquefaction (初期液状化);

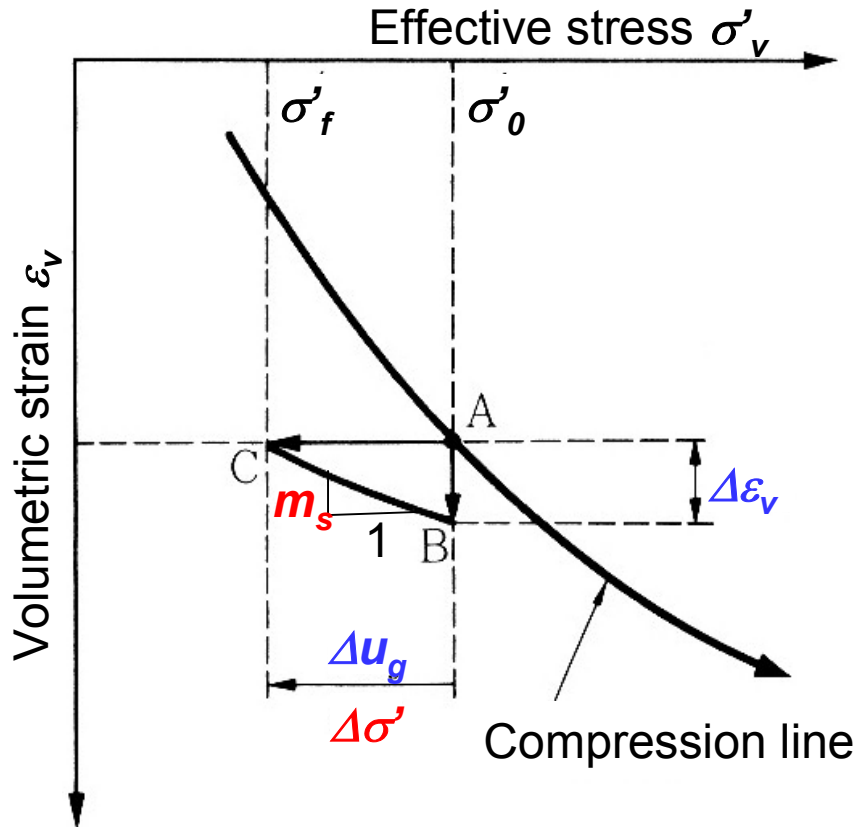
N_f : γ reaches a certain value,
 e.g. DA (double amplitude) = 5%

Definition of liquefaction resistance

液状化強度の定義



Accumulation of Δu in one cycle of loading - Dilatancy and swelling -



- n : porosity;
- m_w : volume compression coef. of water;
- m_s : volume expansion coef. of soil;
- $\Delta\varepsilon_v$: volumetric strain due to one cycle of loading under drained condition;
- Δu_g : generation of Δu due to one cyclic under undrained condition;
- $\Delta\sigma'$: decrease of effective stress.

Considering unit volume of soil under undrained condition,

- change of volume of water: $\Delta u_g m_w n$ ①
- swelling volume of soil due to decrease of effective stress: $m_s \Delta\sigma'$ ②
- volume change of soil $\Delta\varepsilon_v$ -②: $\Delta\varepsilon_v - m_s \Delta\sigma'$ ③ (neglecting volume change of soil grain)
- change of void = volume change of soil:

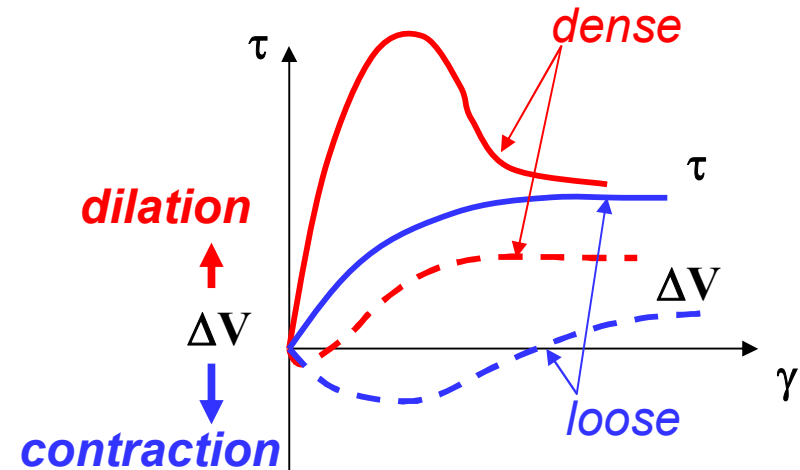
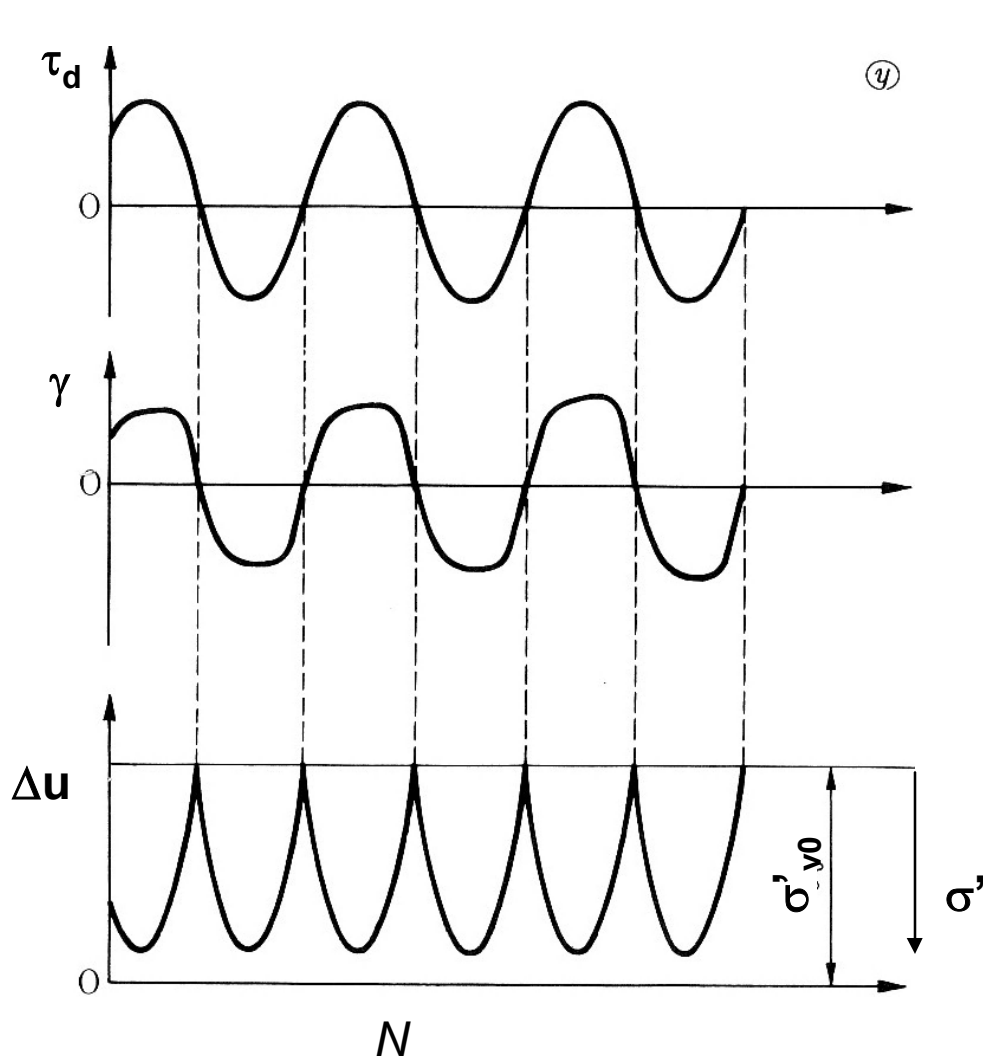
$$\Delta u_g m_w n = \Delta\varepsilon_v - m_s \Delta\sigma' \quad ④$$

$$\Delta u_g = \Delta\sigma' + ④ \Rightarrow \Delta u_g = \frac{\Delta\varepsilon_v}{m_s + m_w n} \quad ⑤$$

$$\Delta u_g \approx \frac{\Delta\varepsilon_v}{m_s}$$

Behavior of **dense** sand subjected to cyclic loading

- **Cyclic mobility** -



Stress and volume change – strain curve of sand in monotonic loading test

Even in dense sand,
contraction takes place at small strain,
=> initial liquefaction ($\sigma' = 0$)
but dilation at large strain,
=> recovery of effective stress and
stiffness, not losing strength.

Factors affecting liquefaction resistance (LR)

Properties of soil

$$\tau_{dl}/\sigma'_{v0}, \sigma_{dl}/2\sigma'_c$$

- Density (D_r);
- Soil type: Grading, Fine contents (F_c), plasticity index (I_p);
- Stress history (OCR), aging effects, microscopic structure (sedimentation process, pre shearing history);

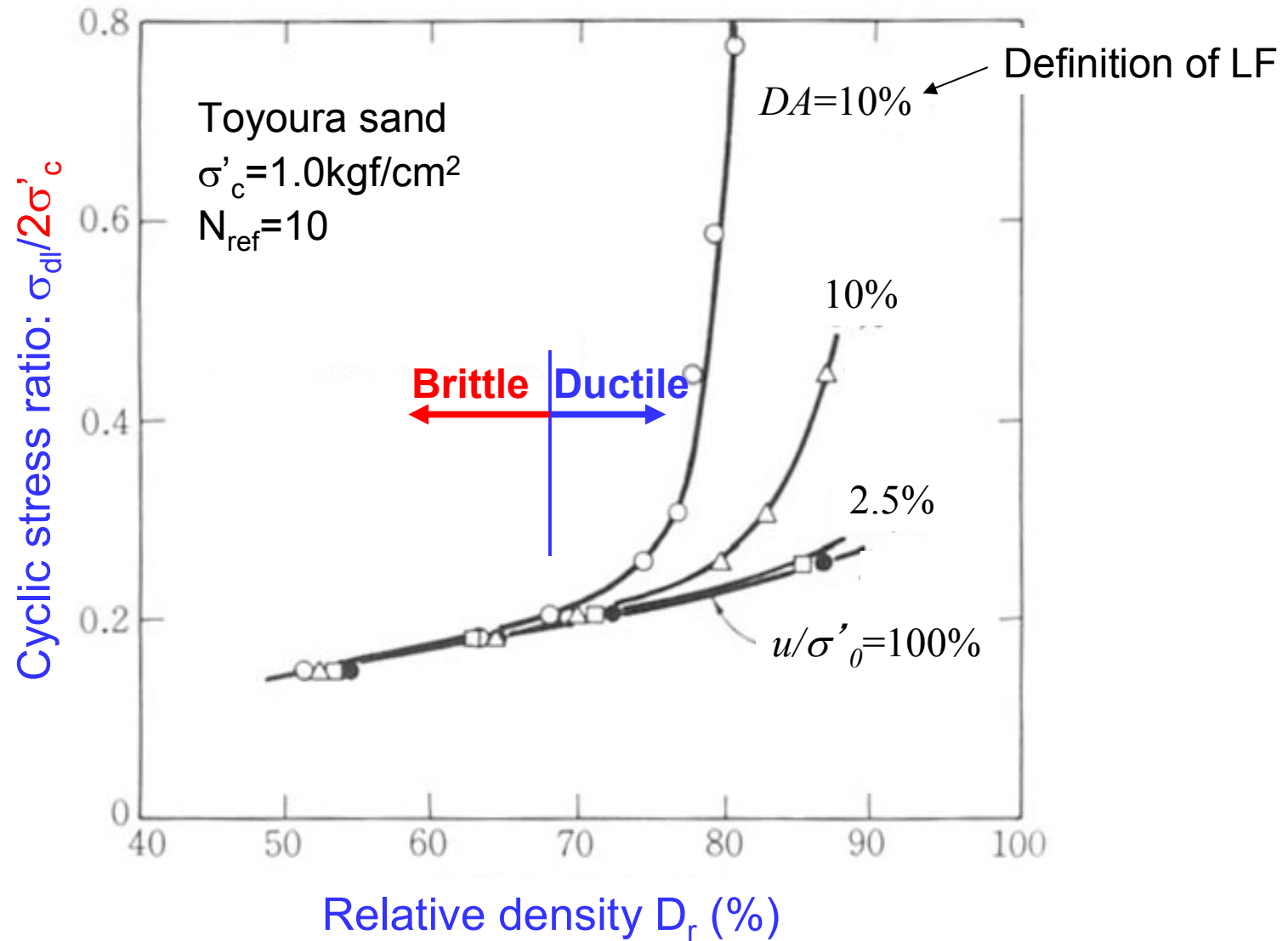
Loading condition, initial stress condition

- Confining pressure (σ'_{v0}, σ'_c);
- Stress Anisotropy under K_0 condition ($\sigma'_h = K_0 \sigma'_v, K_0 \neq 1$);
- Initial shear stress;
- Frequency of cyclic stress;
- Irregularity of seismic loading;
- Multi-directional seismic motion;

Methods of evaluation

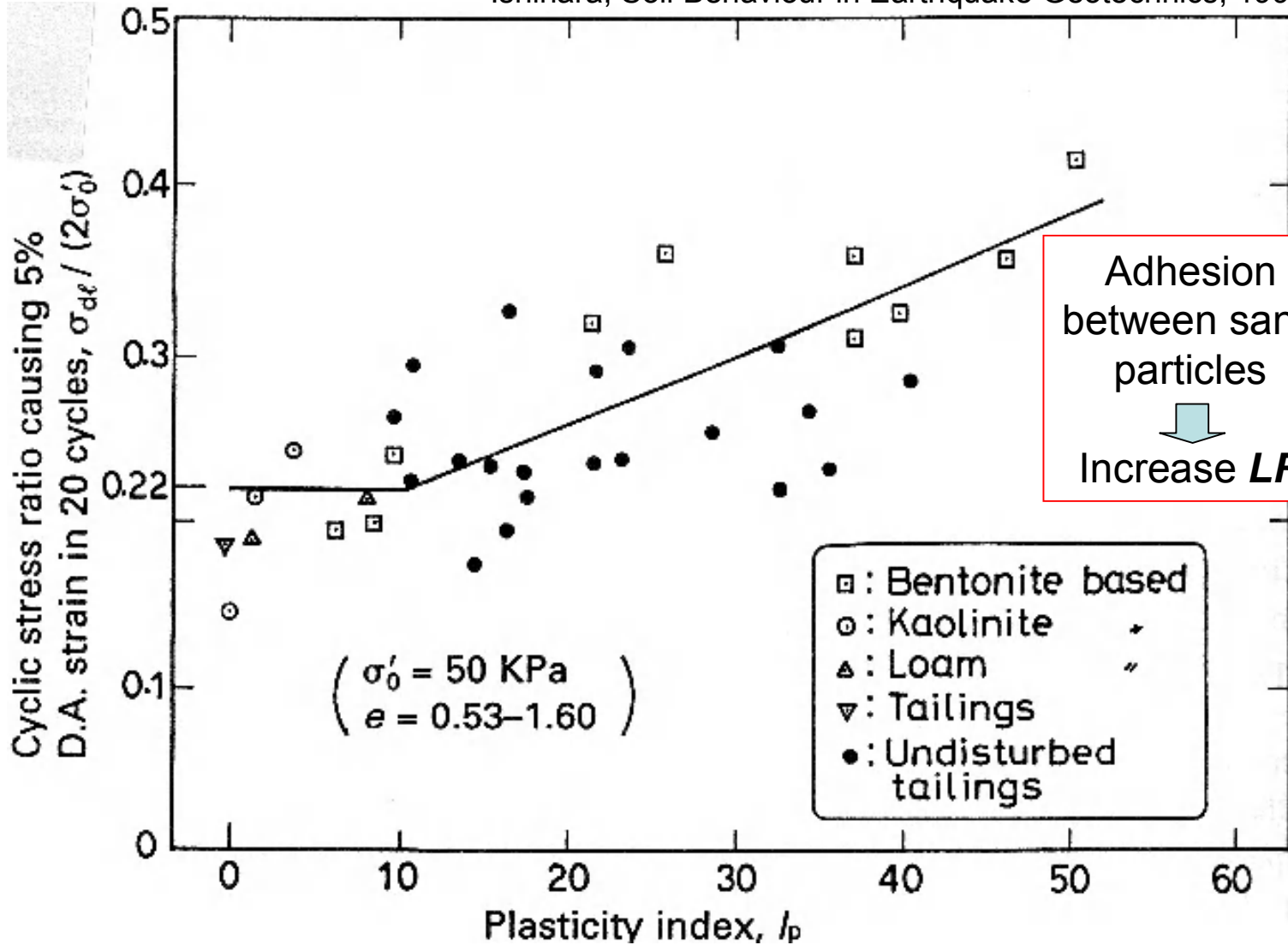
- Sampling disturbance;
- Testing methods (ICT, DSS, HCT);
- Empirical relation of field testing methods (**SPT**, CPT);

Effect of Density



Effect of fine content (F_c), I_p , cohesion

Ishihara, Soil Behaviour in Earthquake Geotechnics, 1996.



Fine particles

cohesion

depending on type of fine

Adhesion between sand particles

Increase **LR**

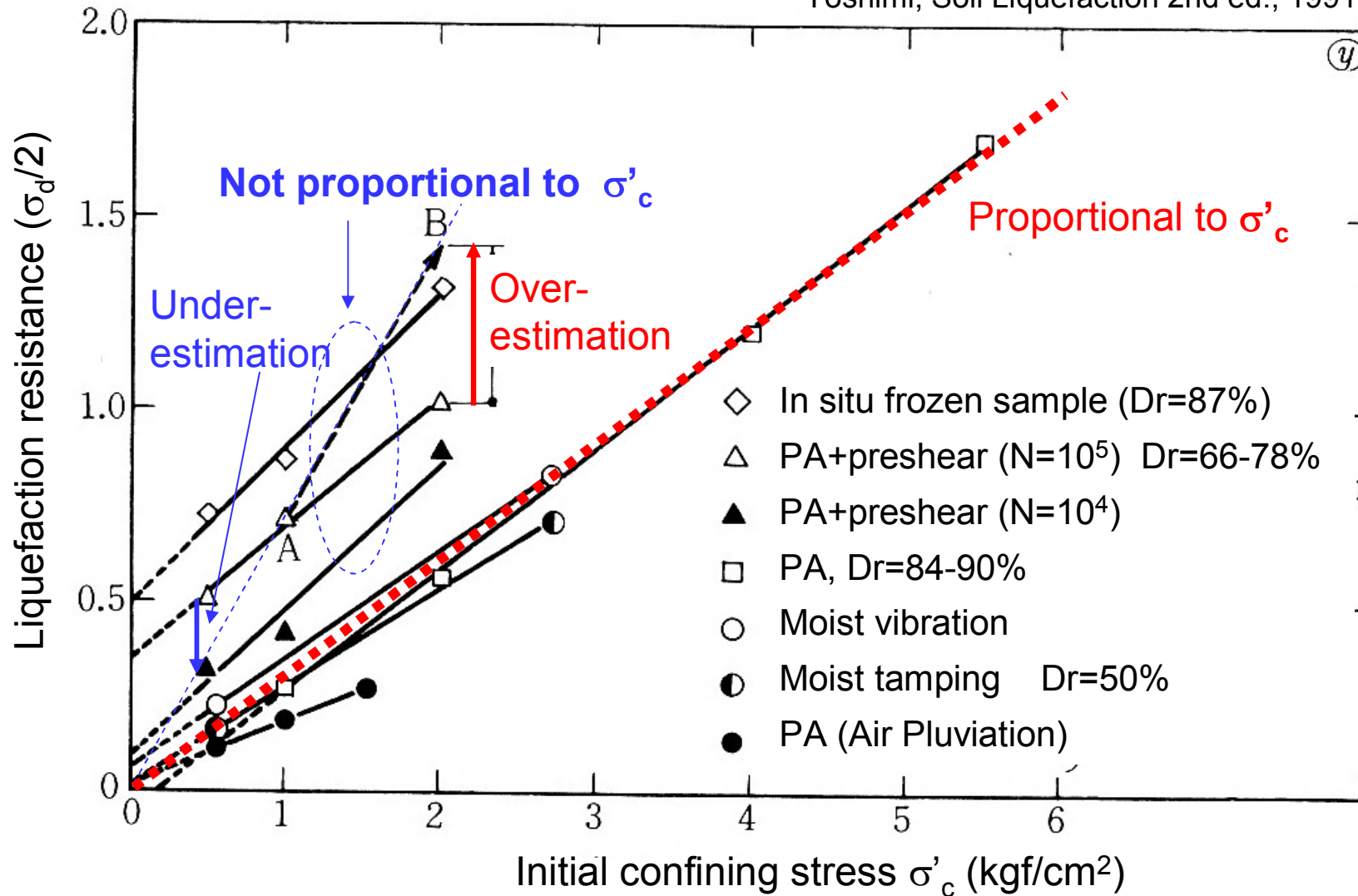
Parameters,

F_c , I_p

Effects of F_c & I_p higher in OC than NC

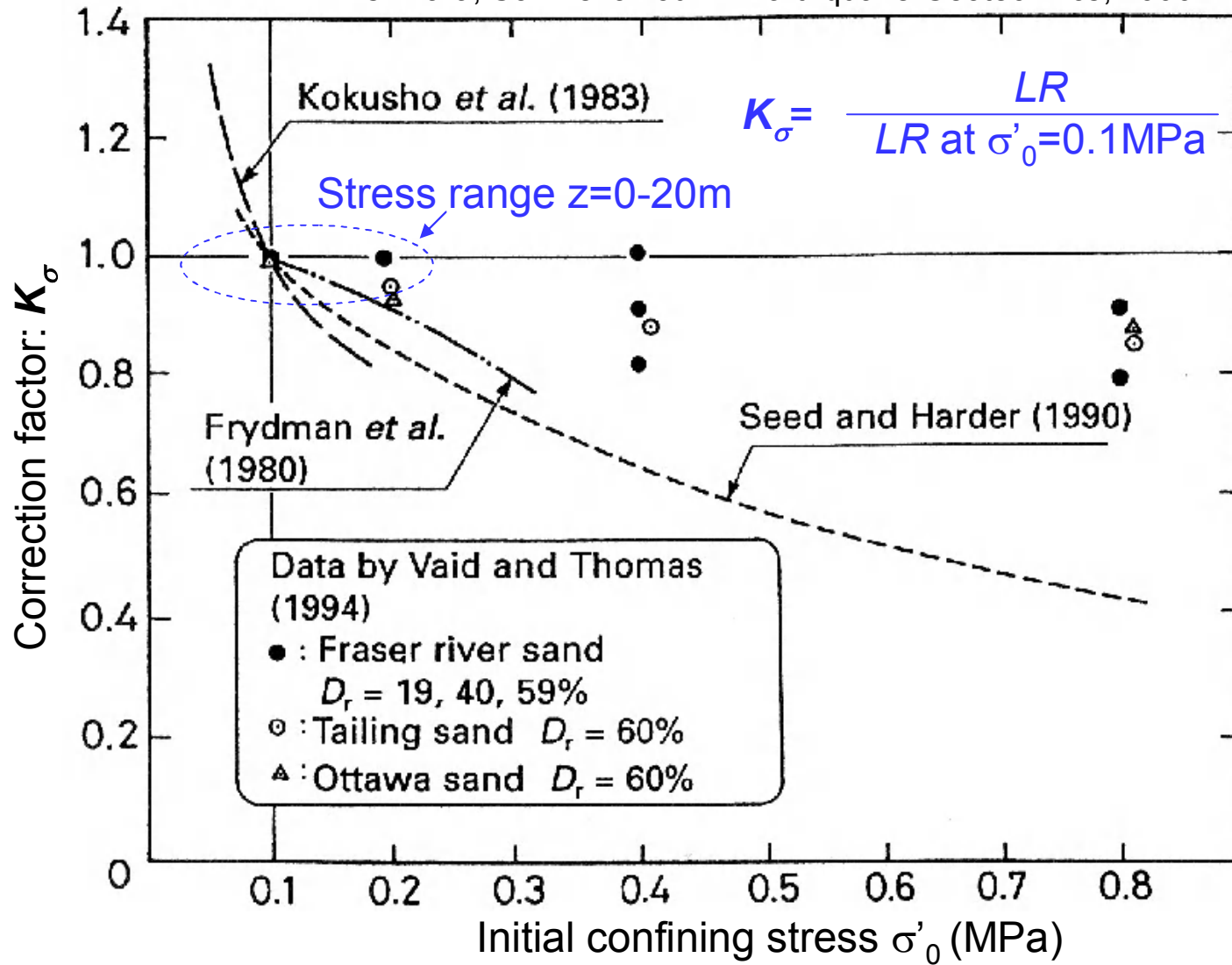
Effect of initial confining pressure:初期拘束圧

Yoshimi, Soil Liquefaction 2nd ed., 1991



Effect of initial confining pressure

Ishihara, Soil Behaviour in Earthquake Geotechnics, 1996.



The higher σ'_c ,
the more contractive.

Lower resistance.

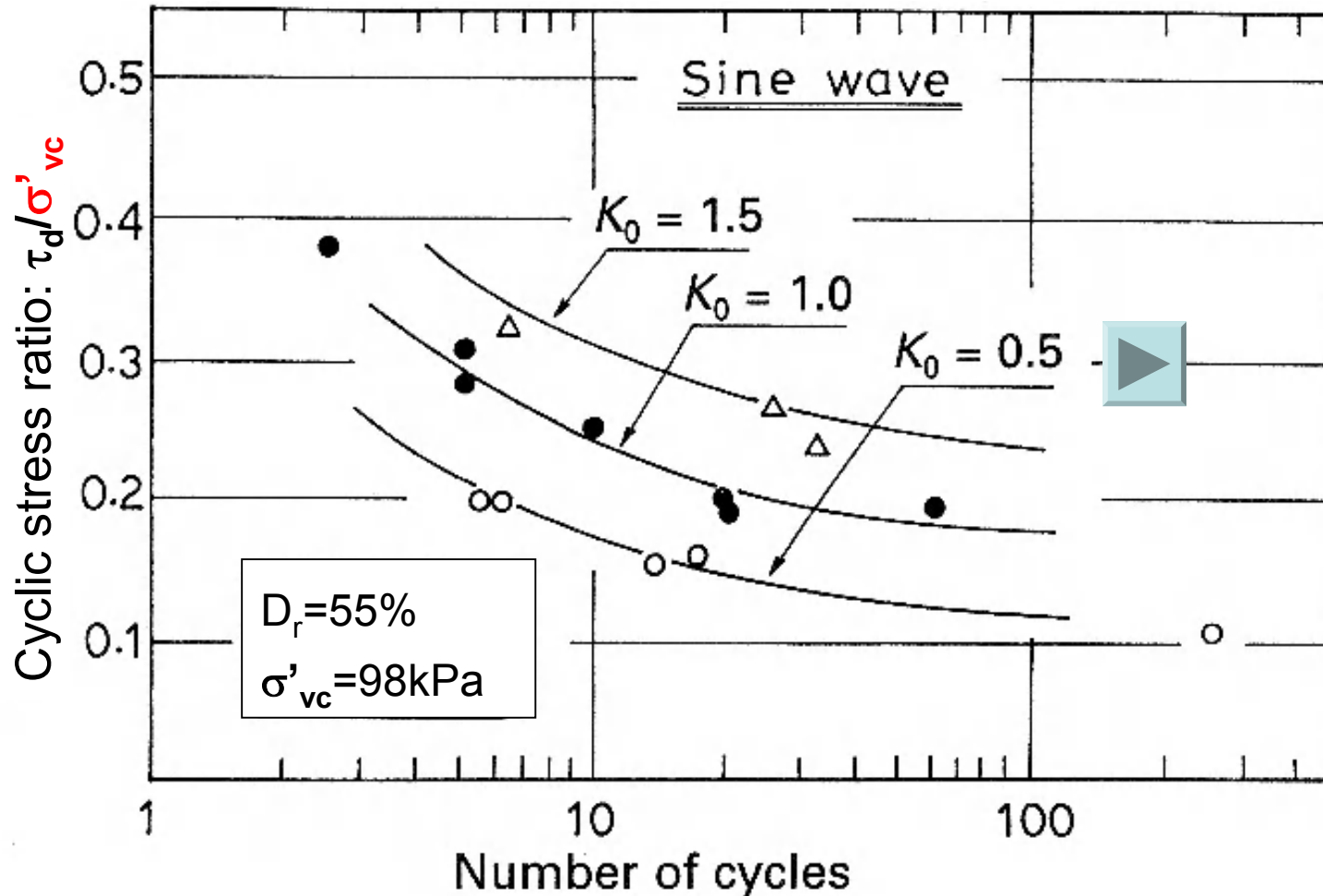
Over estimation for
the case of high
confining stress,
e.g.,
Foundation of Dam.

But not for the level
ground until 20m,
i.e.,
Liquefiable layer.

Justification of
normalized strength
(Liquefaction Resist.)

Effect of K_0 consolidation

Ishihara, Soil Behaviour in Earthquake Geotechnics, 1996.



*The larger K_0 ,
the higher LR.*

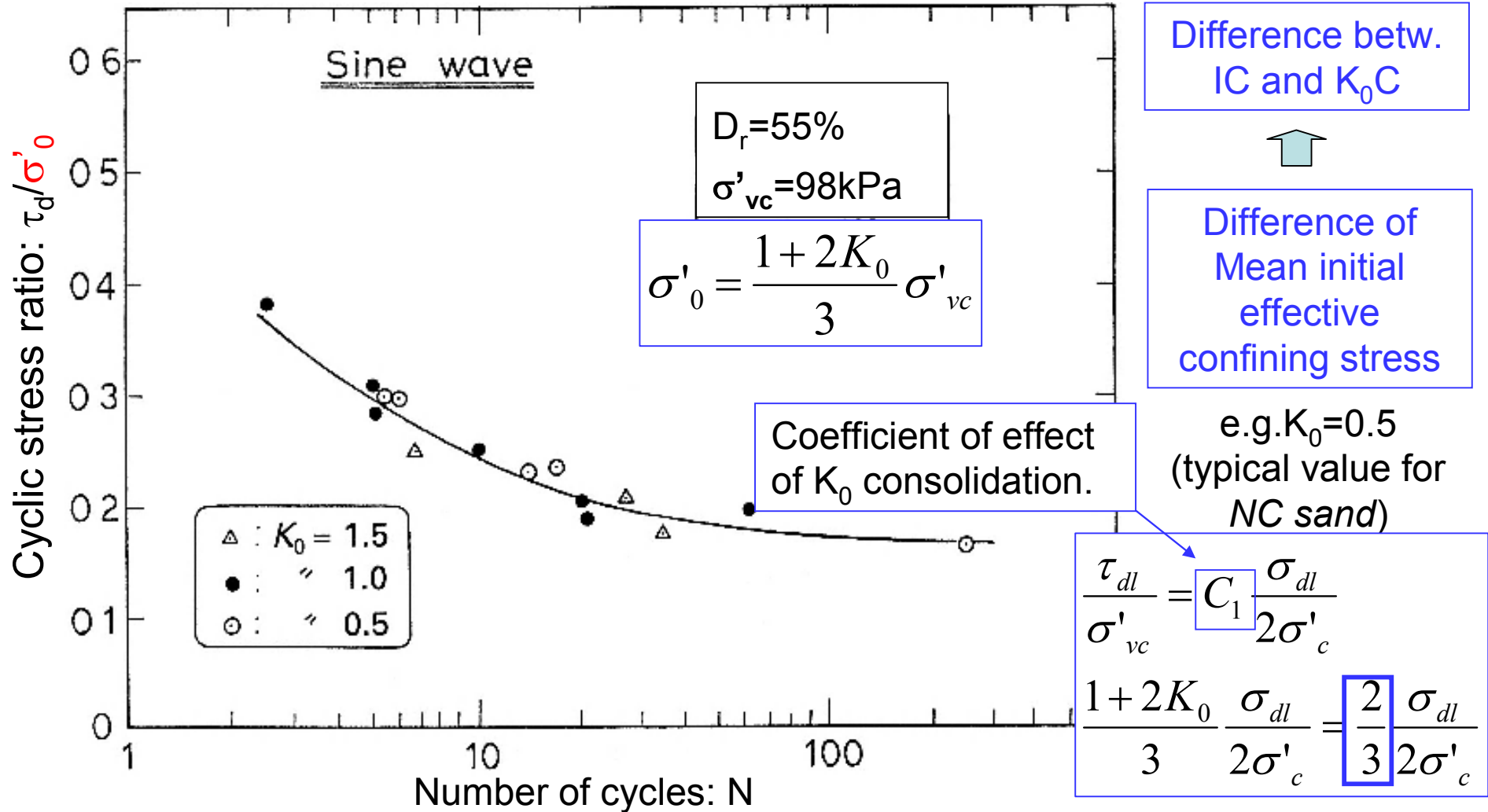


*The larger K_0 ,
the higher mean
effective stress.*

$$\sigma'_0 = \frac{1 + 2K_0}{3} \sigma'_{vc}$$

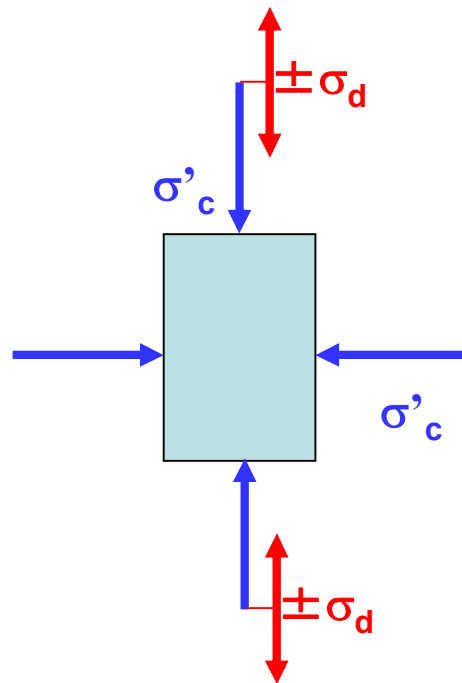
Effect of K_0 consolidation, mean initial effective confining stress

Ishihara, Soil Behaviour in Earthquake Geotechnics, 1996.

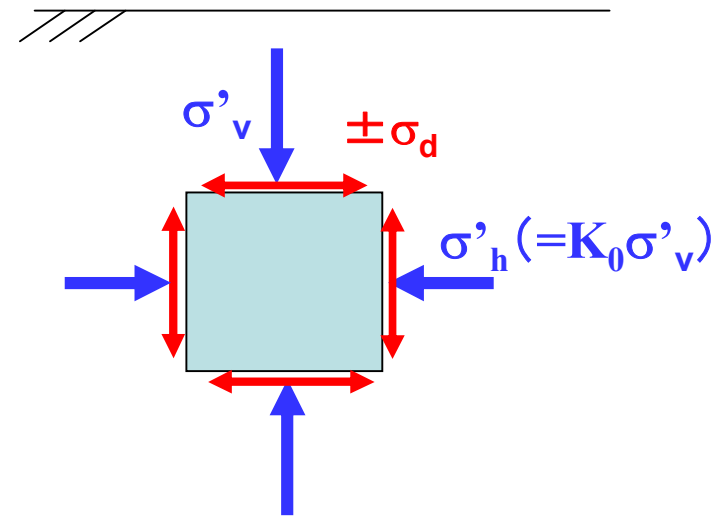


Assignment (due 17 May)

Explain why the normal cyclic triaxial test on isotropically consolidated sample can be used for evaluating liquefaction behaviour of anisotropically consolidated soils in a level ground



normal cyclic triaxial test on isotropically consolidated sample

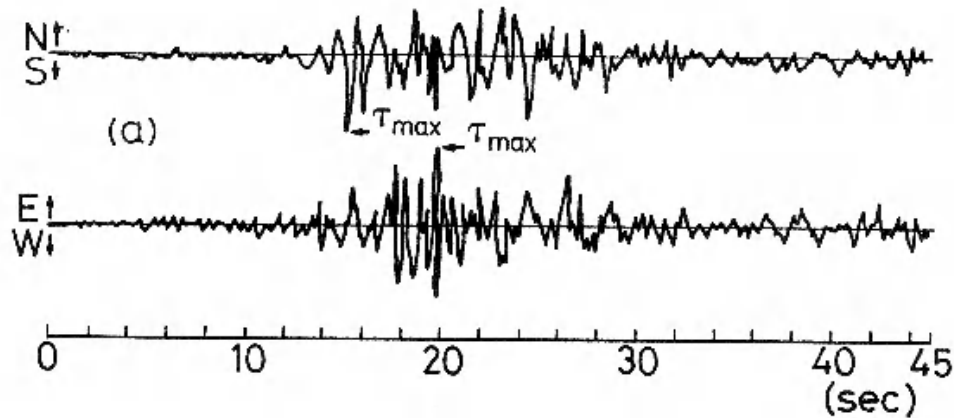


Stress condition of anisotropically consolidated soils in level ground

Effect of irregular seismic loading irregular motion & multi-directionality

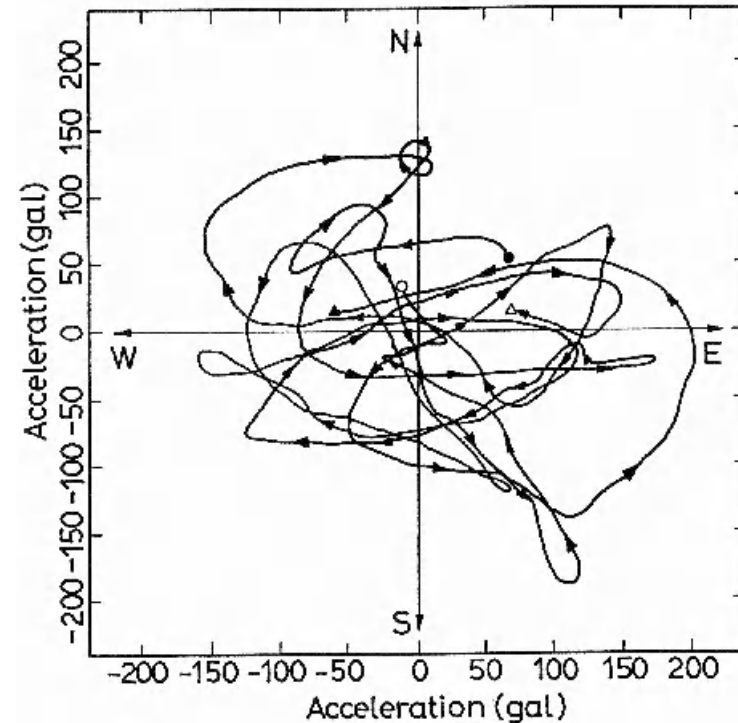
Ishihara, Soil Behaviour in Earthquake Geotechnics, 1996.

Multi-direction, Nihonkai-chubu



Irregular time history

Nihonkai-chubu earthquake of 1983 (Akita)



Trajectory in plan of acceleration time history

Two types of seismic motion:

•Vibration type(振動型):

$$3 \leq (\text{number of } \tau_d > 0.6\tau_{max} \text{ before } \tau_{max})$$

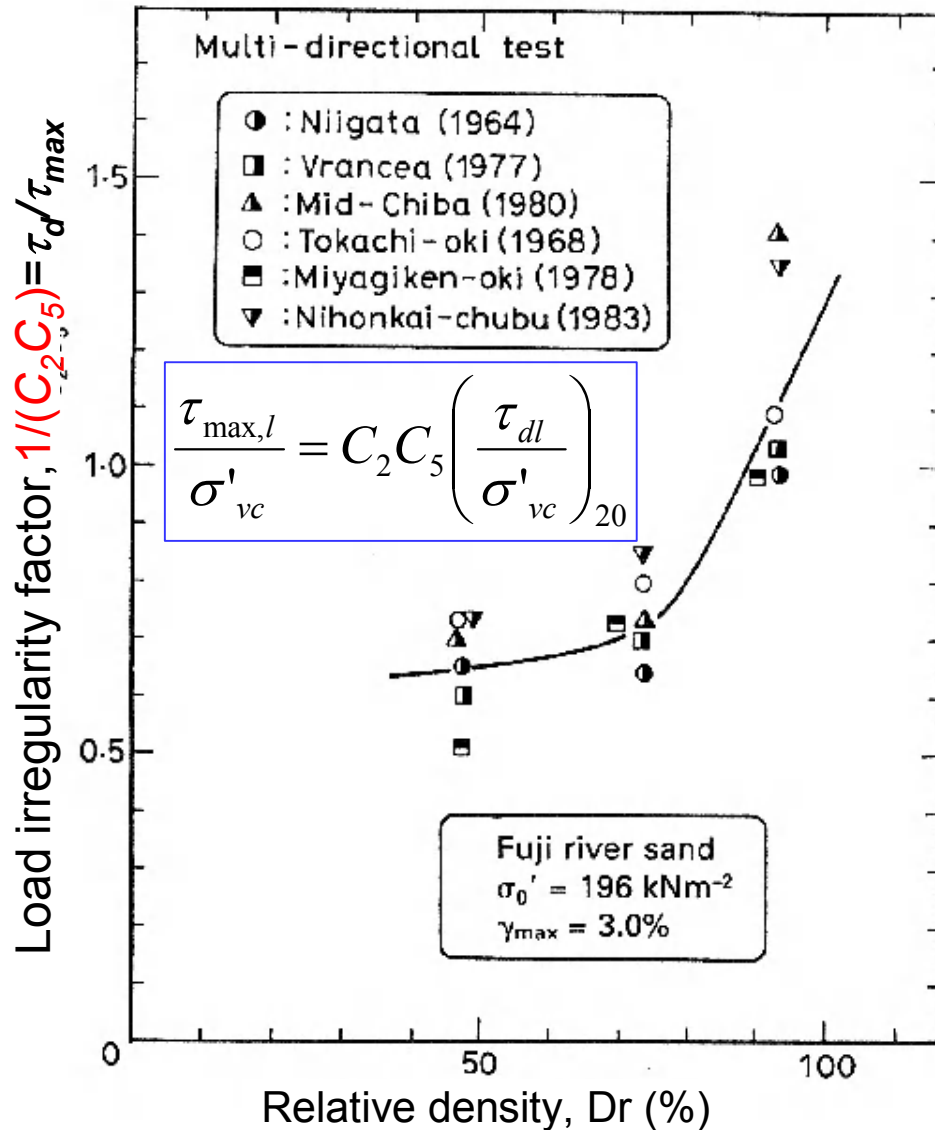
•Impact type(衝撃型):

$$2 \geq (\text{number of } \tau_d > 0.6\tau_{max} \text{ before } \tau_{max})$$

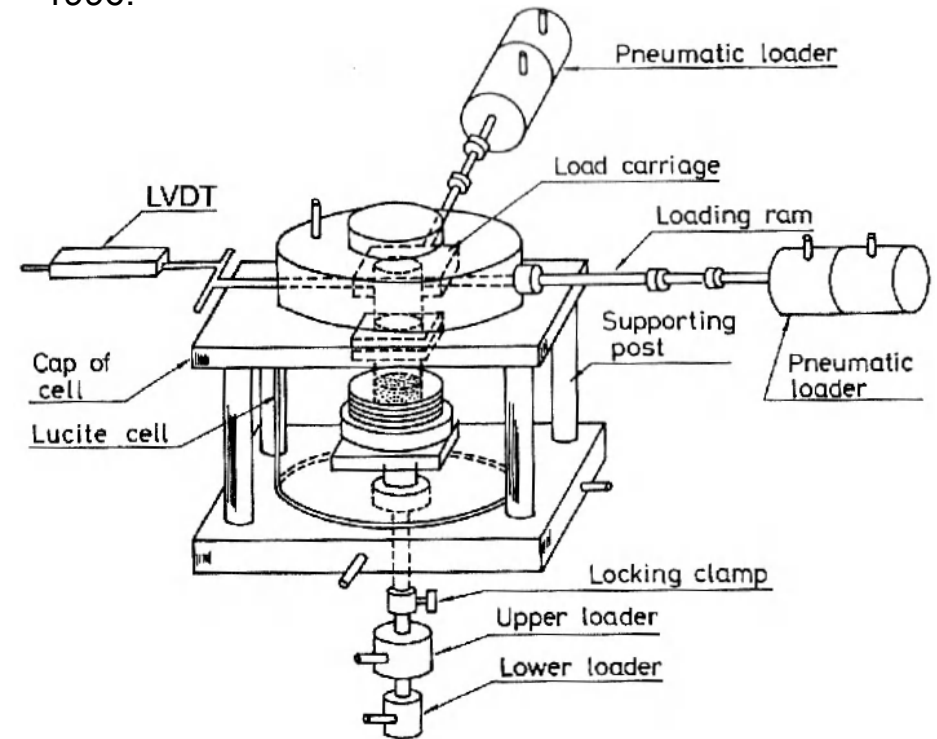
Random ($\tau_{max,l} > (\tau_{d,l})_{20}$) **uniform**

1D ($\tau_{max,l} > \tau_{max,l}$) **2D**

Effect of irregular seismic loading irregular motion & multi-directionality (cont.)

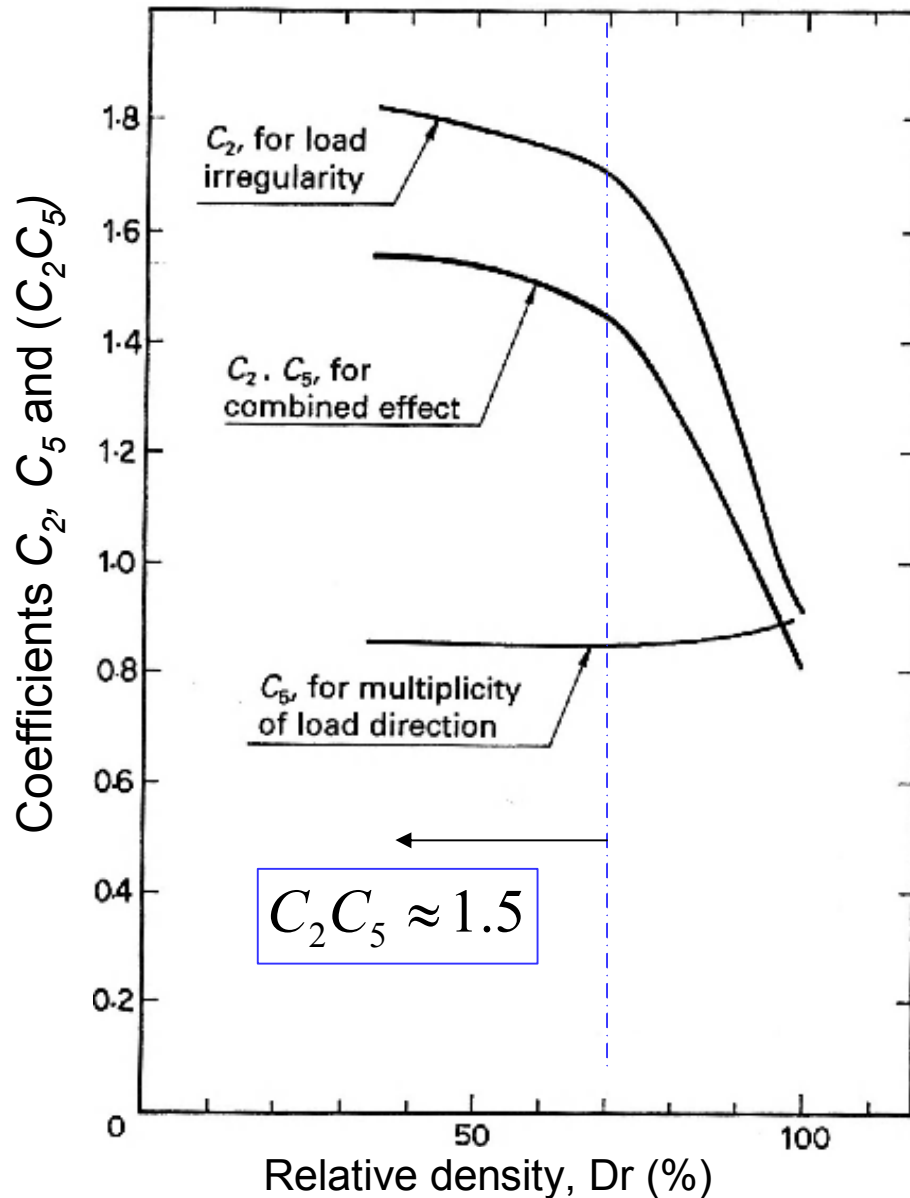


Ishihara, Soil Behaviour in Earthquake Geotechnics, 1996.



C_2 : coefficient on load irregularity
 C_5 : coefficient on multi-directionality

Irregular motion & multi-directionality (cont.)



$$\frac{\tau_{\max,l}}{\sigma'_{vc}} = C_2 C_5 \left(\frac{\tau_{dl}}{\sigma'_{vc}} \right)_{20}$$

$$= C_1 C_2 C_5 \left(\frac{\sigma_{dl}}{\sigma'_c} \right)_{20}$$

$$\frac{\tau_{dl}}{\sigma'_{vc}} = C_1 \frac{\sigma_{dl}}{2\sigma'_c}$$

$$C_1 \approx 2/3$$

$$C_2 C_5 \approx 1.5$$

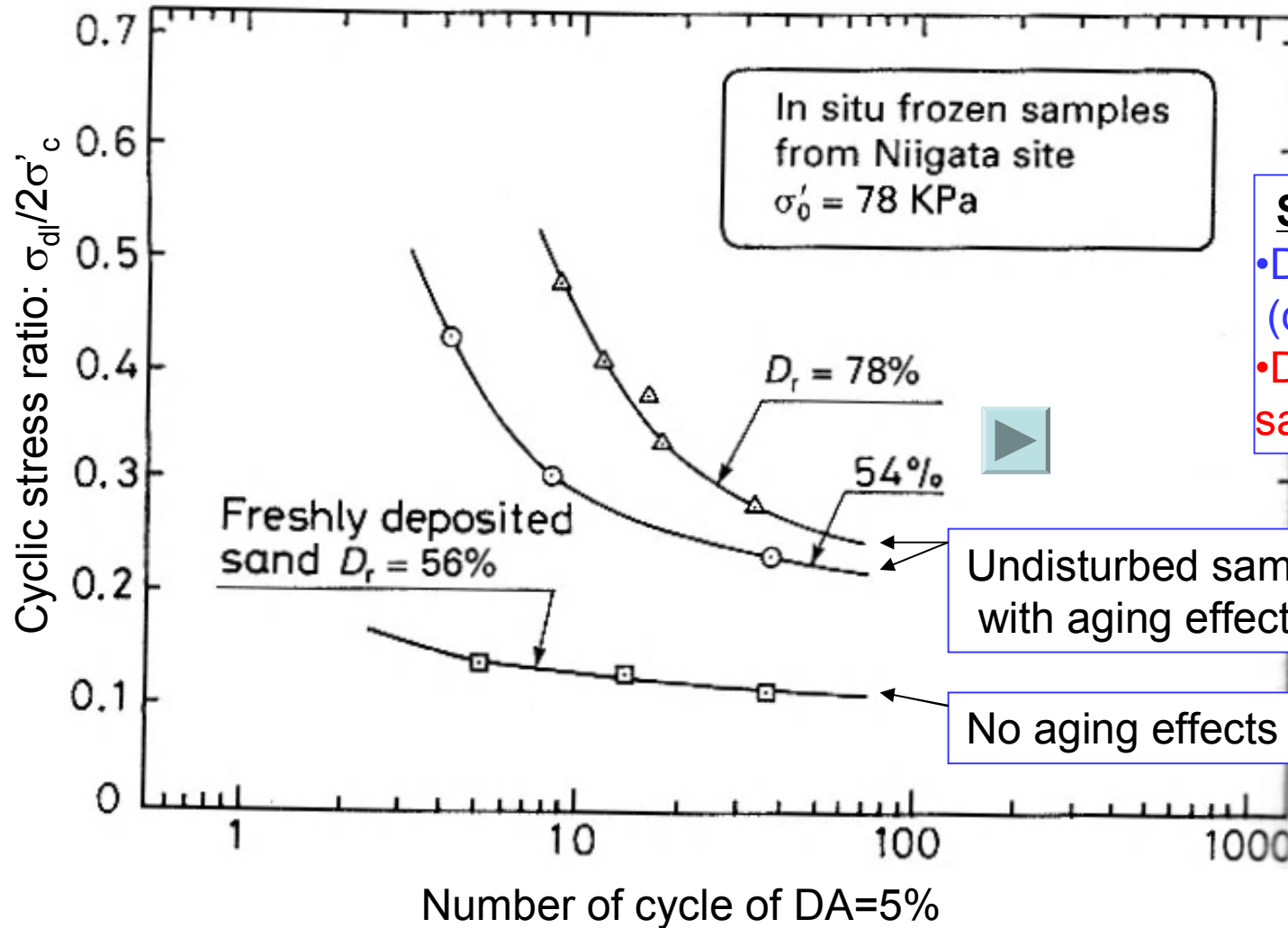
$$\frac{\tau_{\max,l}}{\sigma'_{vc}} \approx \left(\frac{\sigma_{dl}}{2\sigma'_c} \right)_{20}$$

Anisotropic C sample under random irregular loading (real condition)

Isotropic C sample under sinusoidal loading (cyclic triaxial test)

Sampling disturbance

Ishihara, Soil Behaviour in Earthquake Geotechnics, 1996.



Insertion of sampler pre-shear

Sample disturbance

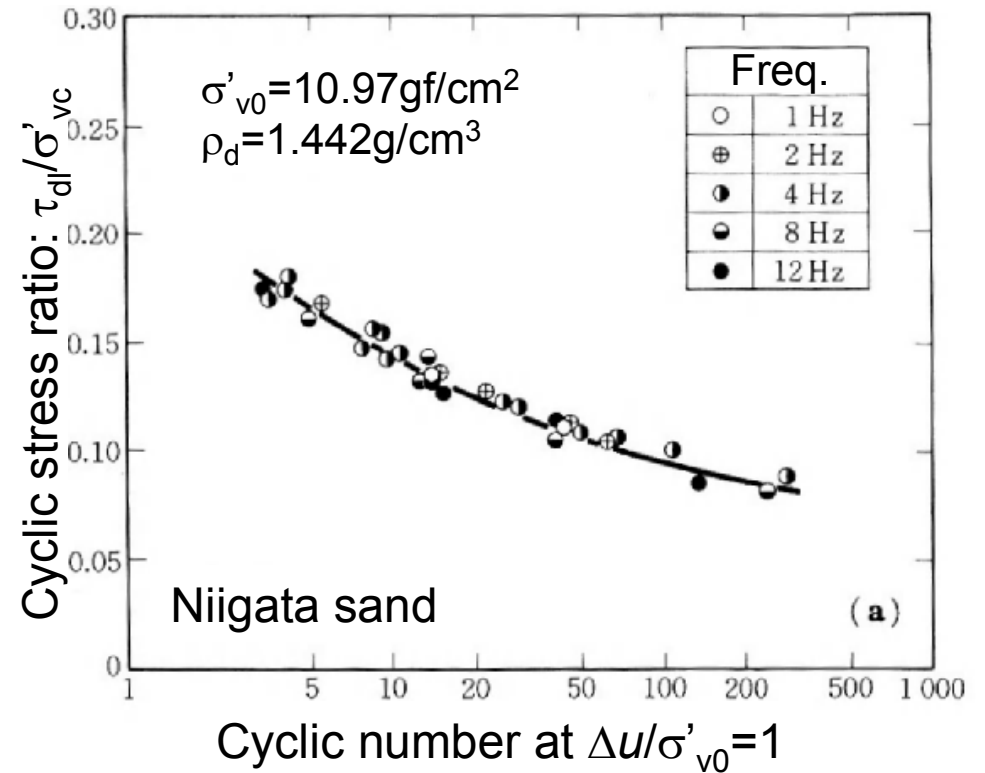
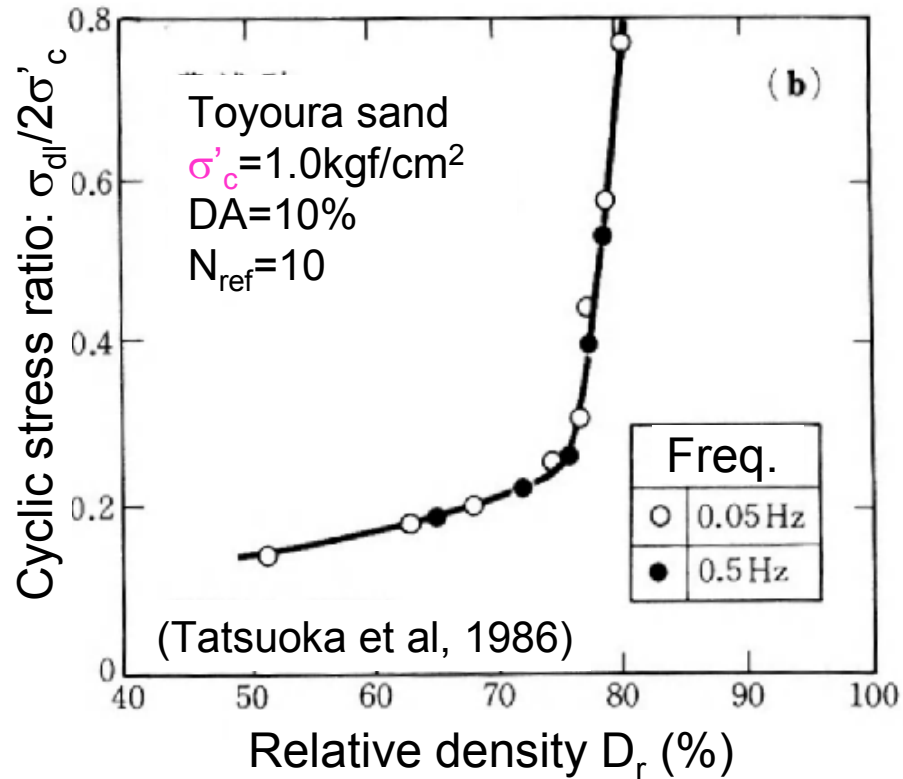
- Destroy aging effects (cementation)
- Densification for loose sand

Undisturbed sample with aging effects

C_3 & C_4 effects

No aging effects

Effect of Frequency



Evaluation of possibility of Liquefaction and its severeness

Liquefaction strength or resistance

+

Cyclic shear stress and cycles

Eq. intensity

Eq. magnitude

Cyclic shear stress caused by earthquake

Equation of shear vibration

$$\frac{\gamma}{g} \frac{\partial^2 u}{\partial t^2} = \frac{\partial \tau}{\partial z}$$

$$\int_0^z \frac{\partial \tau}{\partial z} dz = \tau(z, t) = \int_0^z \frac{\gamma}{g} \frac{\partial^2 u}{\partial t^2} dz$$

where $\frac{\partial^2 u}{\partial t^2} = \alpha(z, t)$

If the ground is rigid, $u(z, t) \Rightarrow u(t)$

$$\tau(z, t) = \frac{\alpha(t)}{g} \int_0^z \gamma(z) dz = \frac{\alpha(t)}{g} \sigma_v$$

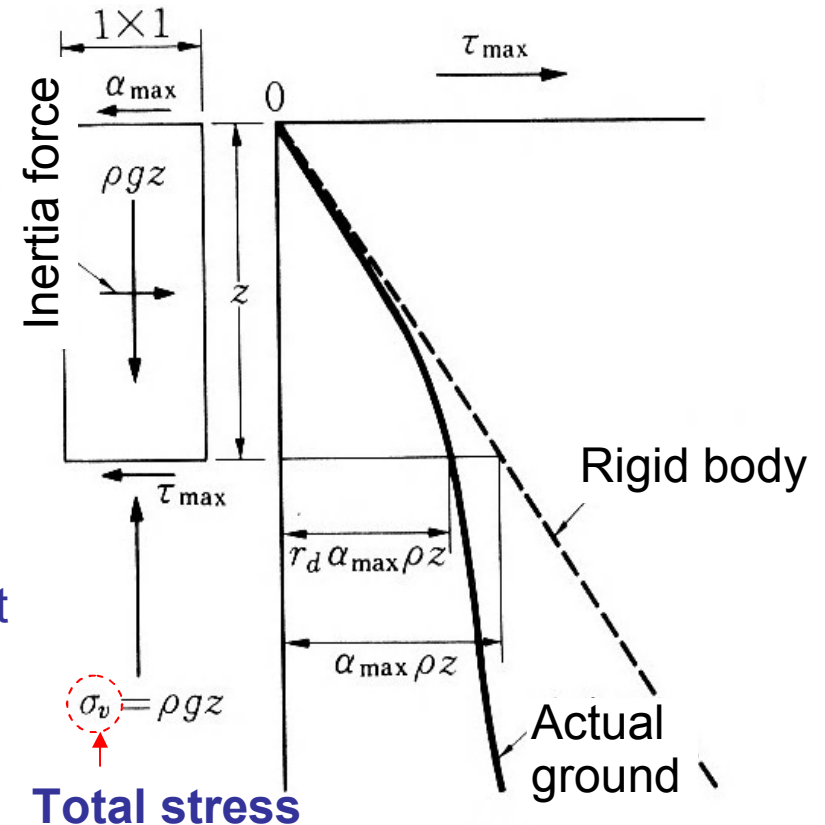
$$\tau_{\max}^r = \text{Max } \tau(z, t) = \frac{\alpha_{\max}}{g} \sigma_v$$

Shear stress ratio

$$\tau_{\max} = \frac{\alpha_{\max}}{g} r_d \gamma_t z$$

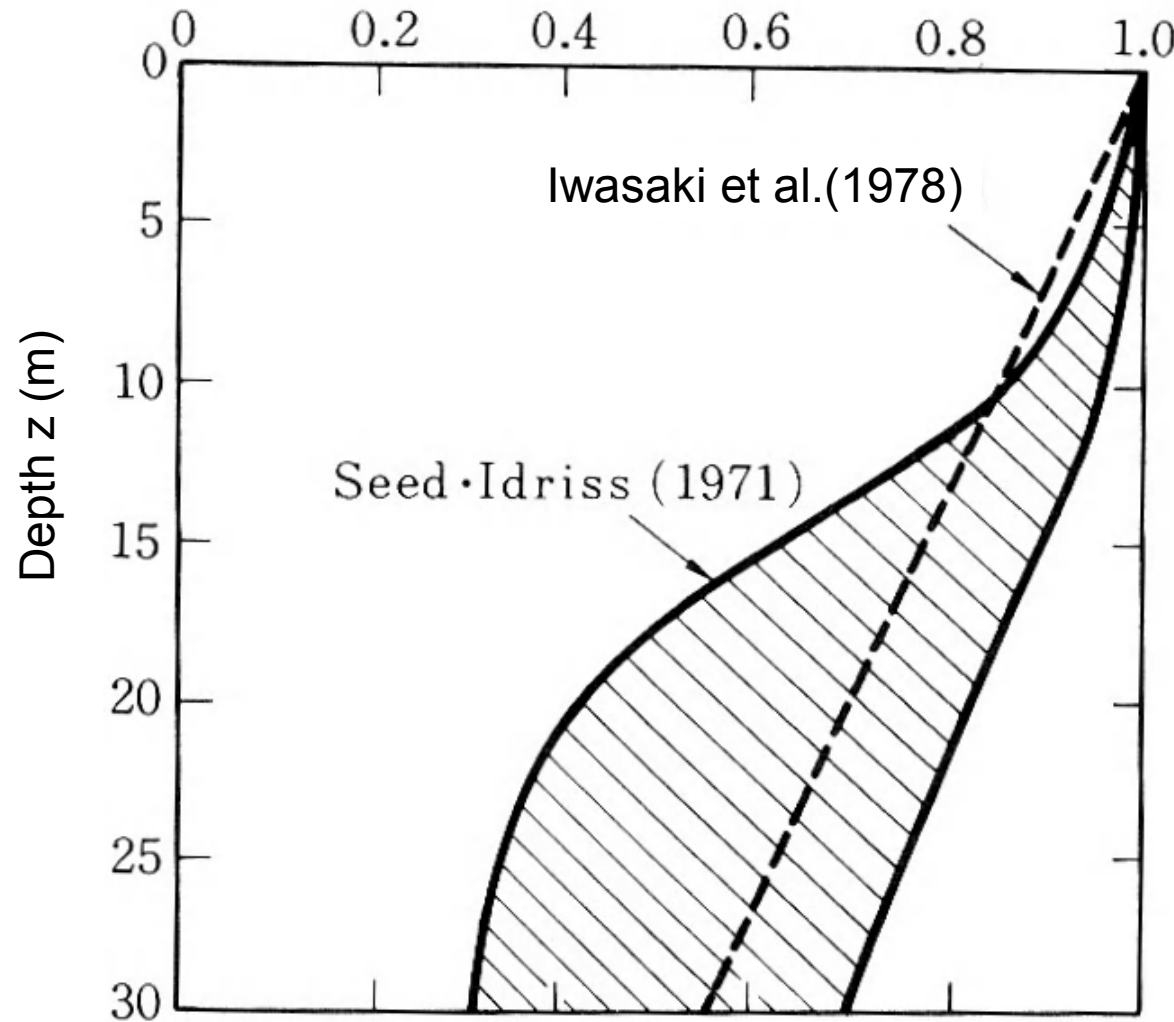
$$\frac{\tau_{\max}}{\sigma'_v} = \frac{\alpha_{\max}}{g} r_d \frac{\sigma_v}{\sigma'_v}$$

Total unit weight



Stress reduction factor

$$r_d = \frac{\tau_{\max}}{\left(\frac{\alpha_{\max}}{g} \right) \sigma_v}$$



Factor of safety: F_L

Liquefaction resistance : $R = \frac{\tau_{\max,l}}{\sigma'_v}$

Maximum stress ratio : $L = \frac{\tau_{\max}}{\sigma'_v} = \frac{\alpha_{\max}}{g} r_d \frac{\sigma_v}{\sigma'_v}$

$$F_L = \frac{R}{L} = \frac{\tau_{\max,l} / \sigma'_v}{\tau_{\max} / \sigma'_v}$$

•Reduction of mechanical properties of soils and design parameter

Liquefaction potential: P_L

$$P_L = \int_0^{20} (1 - F_L) \underbrace{(10 - 0.5z)}_{\text{Weighing coefficient for depth: (below 20m, no liquefaction)}} dz$$

Weighing coefficient for depth:
(below 20m, no liquefaction)

•Design of pile foundation
•Assessment of stability of oil tank

Assessment of F_L

Simplified methods

R: Field Test

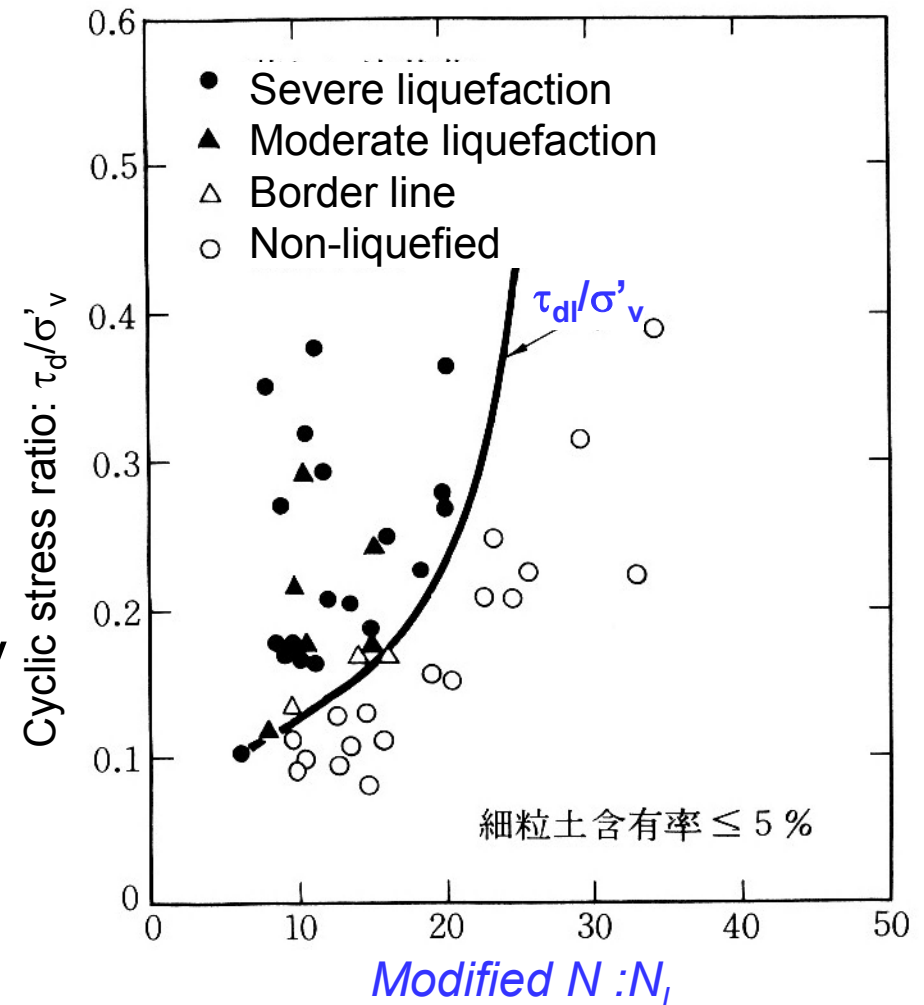
(**N-value**, cone resistance)
correction for various factors

- Seed' method:
- Specification of Highway Bridge
- Eq. Resist. Design of Port Facility
(Critical N-value)

Precise method (not common)

R: sampling + lab test (?)

L: dynamic response analysis

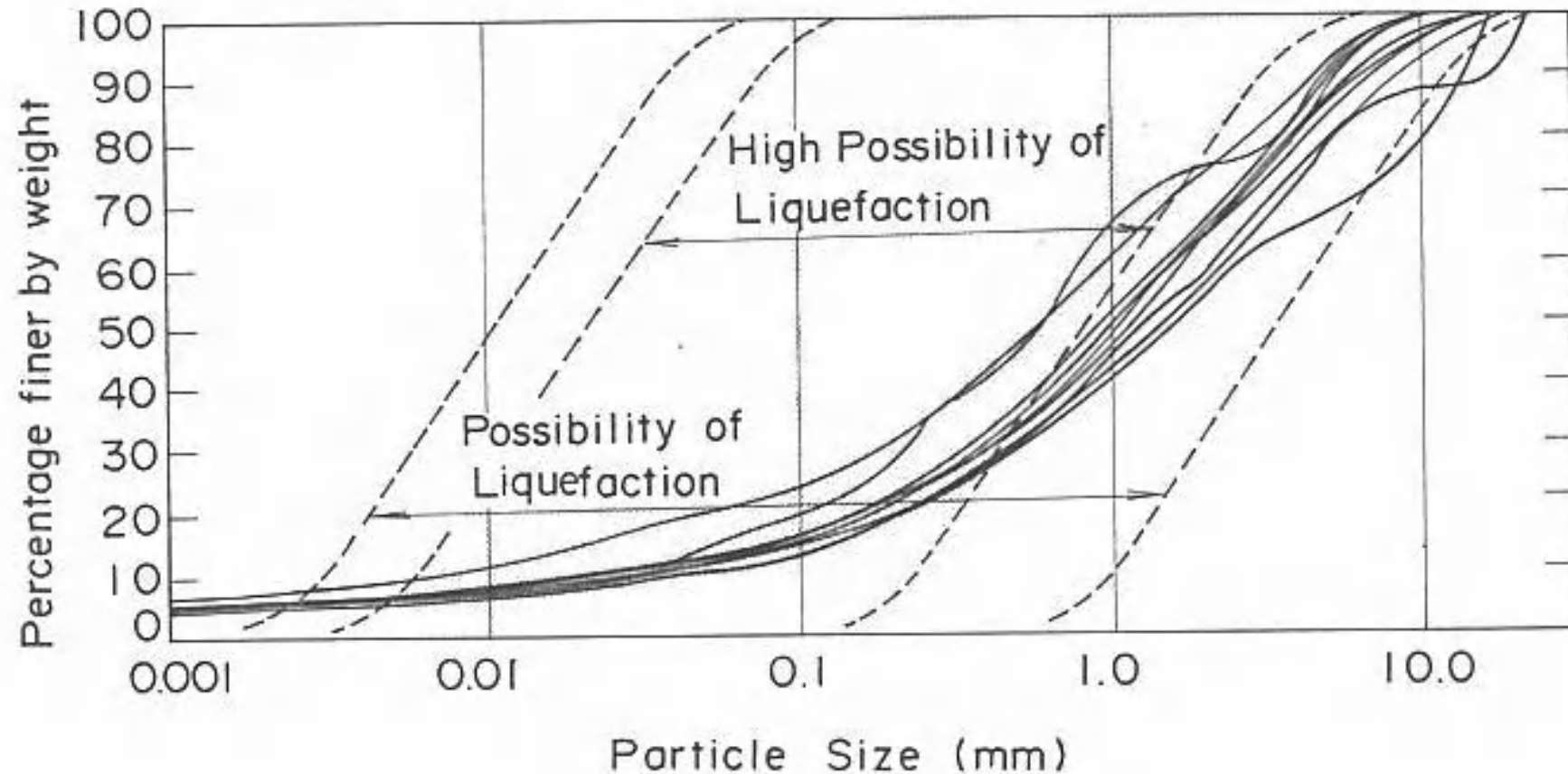


$$N_1 = \frac{1.7}{0.7 + \sigma'_v}, \sigma'_v : \text{kg/cm}^2$$

Conditions of Liquefaction

- **Cyclic shear deformation**
- Uniformly graded **sand ground??**
 - silt or clay exhibits no dilatancy behavior
 - liquefaction is not sustainable in gravel
(high permeability prevents the accumulation of Δu)
- **particle size and distribution**
- **Loose ground**
 - loose grounds show large volume reduction
- High level of ground water table (**Saturation**)
 - liquefaction is not sustainable in dry condition
 - ground water keeps liquefaction

Grading curve of decomposed granite (Masado) used for landfill



Liquefiable Grounds and Soil Structures

- Loosely deposited sand at **river side or sea side**
- **Reclaimed ground** in port and harbor areas
- Embankments filled loosely
 - road, railway, river dike, housing lots, dam

Comparison of liquefaction assessment in Highway bridge specifications in 1990 and 1996

Liquefiable soil layer

1990 version	1996 version
<p>Alluvial sand layers which satisfy</p> <ol style="list-style-type: none"> 1. Water table less than 10m from the ground surface. 2. Depth less than 20m from GS 3. $0.02\text{mm} \leq D_{50} \leq 2.0\text{mm}$ 	<p>Alluvial sand layers which satisfy</p> <ol style="list-style-type: none"> 1. Water table less than 10m from the ground surface. 2. Depth less than 20m from GS 3. Either $F_c \leq 35\%$ or $I_p \leq 15$ 4. $D_{50} \leq 10\text{mm}$ and $D_{10} \leq 1\text{mm}$

Liquefaction occurrence

Liquefy when $F_L \leq 1$, where $F_L = R/L$

Comparison of liquefaction assessment in Highway bridge specifications in 1990 and 1996 (cont.)

Cyclic Shear resistance ratio, R 1990 version

$$R = C_1 \cdot C_2 \cdot C_3 \cdot C_4 \cdot C_5 \cdot R_L$$

$$R_L = R_1 + R_2 + R_3$$

R_L : liquefaction strength obtained by triaxial test

$$R_1 = 0.0882 \sqrt{\frac{N}{\sigma'_v + 0.7}} \quad \sigma'_v \Rightarrow \text{unit: kgf/cm}^2$$

C_1, C_2, C_3, C_4, C_5 :
correction factors

$$R_2 = \begin{cases} 0.19 & (0.02mm \leq D_{50} \leq 0.05mm) \\ 0.225 \log_{10} \left(\frac{0.35}{D_{50}} \right) & (0.05mm \leq D_{50} \leq 0.6mm) \\ -0.05 & (0.6mm \leq D_{50} \leq 2.0mm) \end{cases}$$

$$R_3 = \begin{cases} 0.0 & (0\% \leq F_c \leq 40\%) \\ 0.004F_c - 0.16 & (40\% \leq F_c \leq 100\%) \end{cases}$$

Comparison of liquefaction assessment in Highway bridge specifications in 1990 and 1996 (cont.)

Cyclic Shear resistance ratio, R **1996 version**

$$R = C_1 \cdot C_2 \cdot C_3 \cdot C_4 \cdot C_5 \cdot R_L$$

R_L : liquefaction strength obtained by triaxial test

C_1, C_2, C_3, C_4, C_5 :
correction factors

$$R_L = \begin{cases} 0.0882 \sqrt{\frac{N_a}{1.7}} & (N_a < 14) \\ 0.0882 \sqrt{\frac{N_a}{1.7}} + 1.6 \times 10^{-6} \cdot (N_a - 14)^{4.5} & (14 \leq N_a) \end{cases}$$

Sandy soils N_1 : Equivalent N-value at 1kgf/cm² of effective overburden stress (σ'_v)

$$N_a = aN_1 + b \quad \leftarrow N_a: \text{Corrected N-value}$$

$$N_1 = 1.7N / (\sigma'_v + 0.7)$$

$$a = \begin{cases} 1 & (0\% \leq F_c < 10\%) \\ (F_c + 40) / 50 & (10\% \leq F_c < 60\%) \\ F_c / 20 - 1 & (60\% \leq F_c) \end{cases}$$

$$b = \begin{cases} 0 & (0\% \leq F_c < 10\%) \\ (F_c - 10) / 18 & (10\% \leq F_c) \end{cases}$$

Gravelly soils

$$N_a = (1 - 0.36 \log_{10}(D_{50} / 2)) N_1$$

Comparison of liquefaction assessment in Highway bridge specifications in 1990 and 1996 (cont.)

Correction from the strength under triaxial conditions to that in-situ

1990 version

$$C_1 \cdot C_2 \cdot C_3 \cdot C_4 \cdot C_5 = 1.0$$

C_1 : difference of confining stress between triaxial condition (isotropic) and in-situ(K_0)

C_2 : Irregularity of earthquake wave

C_3 : Disturbance from sampling to test

C_4 : Densification from sampling to test

C_5 : Multi-directional characteristics of ground shaking

1996 version

C_1, C_2, C_3, C_4, C_5 : same as 1990 version

$$C_3 \cdot C_4 \cdot C_5 = 1.0$$

$$C_w = C_1 \cdot C_2$$

<Type -1 earthquake motion> **tectonic type**

$$C_w = 1.0$$

<Type -2 earthquake motion> **near-field**

$$C_w = \begin{cases} 1.0 & (R_L \leq 0.1) \\ 3.3R_L + 0.67 & (0.1 \leq R_L \leq 0.4) \\ 2.0 & (0.4 < R_L) \end{cases}$$



Comparison of liquefaction assessment in Highway bridge specifications in 1990 and 1996 (cont.)

Shear stress ratio during an earthquake, L

1990 version

$$L = r_d \cdot k_s \cdot \frac{\sigma_v}{\sigma'_v}$$

$$k_s = c_z \cdot c_G \cdot c_I \cdot k_{s0}$$

- r_d : Reduction factor of the shear stress ratio with depth
- k_s : Horizontal seismic coefficient at the ground surface
- c_z : Seismic zone factor
- c_G : Ground condition factor
- c_I : Factor on the importance of the structure
- k_{s0} : Standard horizontal seismic coefficient (0.15)

1996 version

$$L = r_d \cdot k_{hc} \cdot \frac{\sigma_v}{\sigma'_v}$$

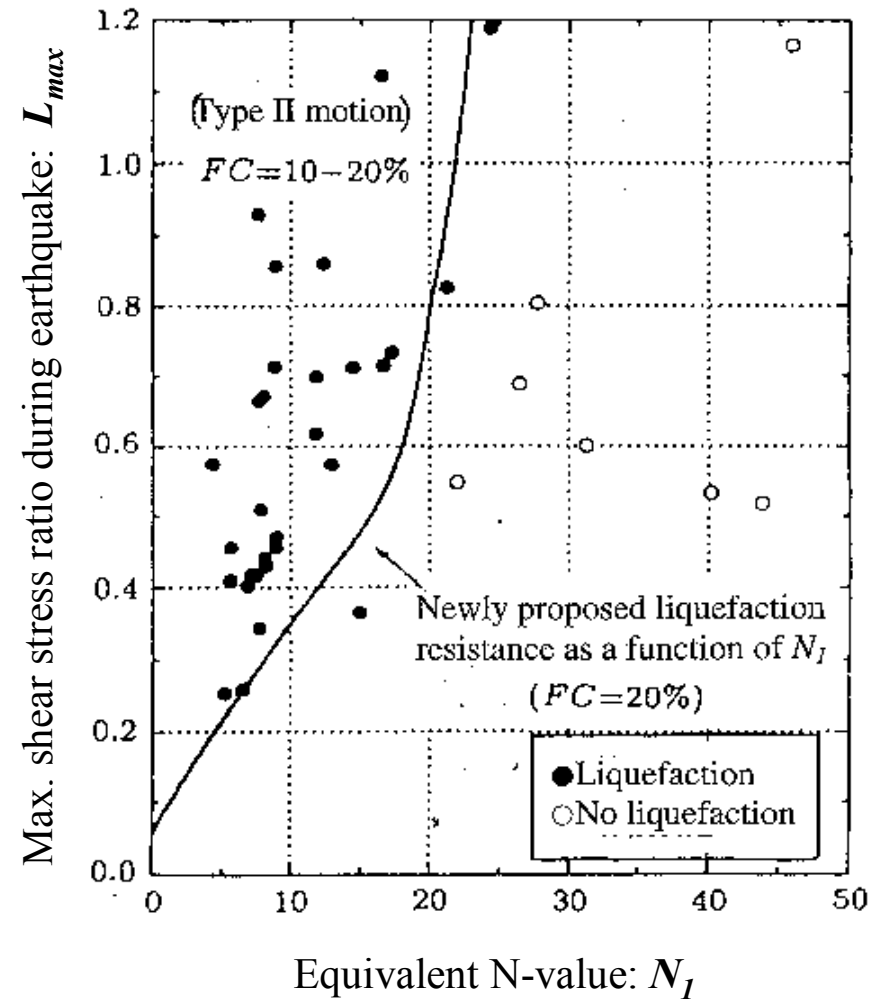
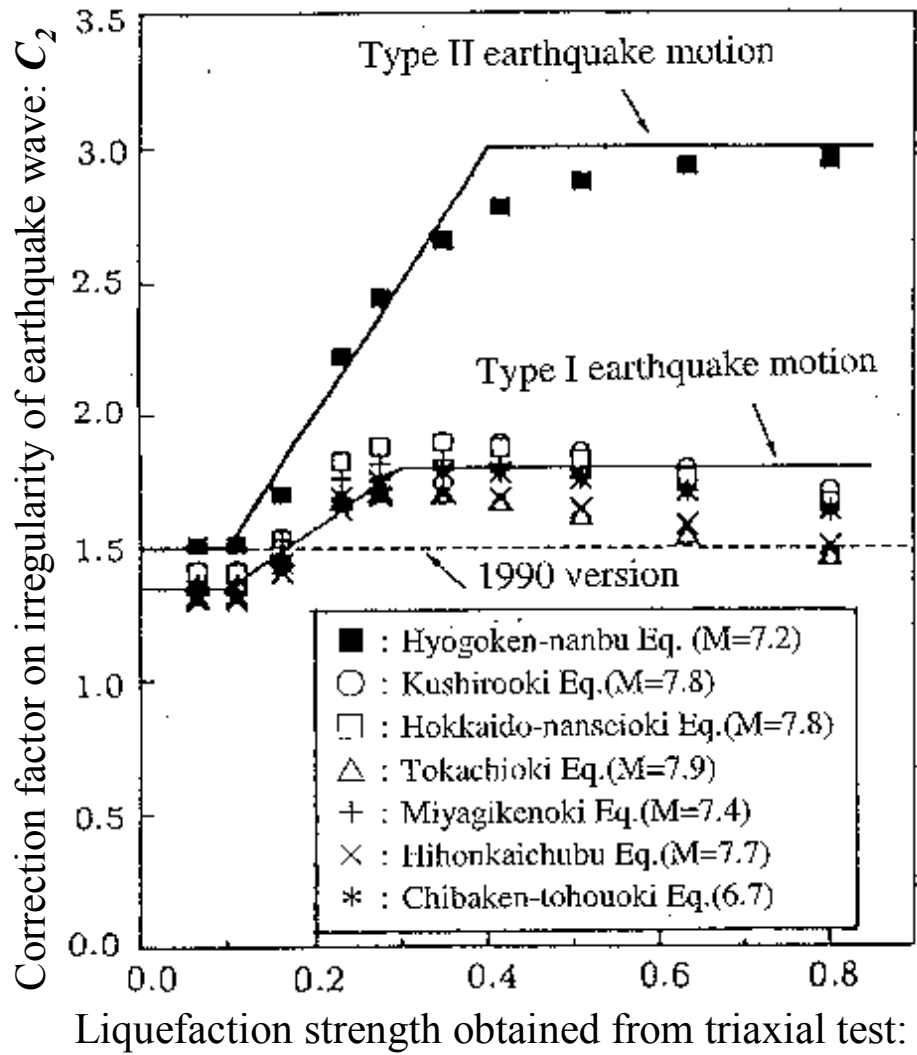
$$k_{hc} = c_z \cdot k_{s0}$$

- k_{hc} : Horizontal seismic coefficient at the ground surface
- c_z : Seismic zone factor
- c_G : Ground condition factor
- k_{s0} : Standard horizontal seismic coefficient shown in the following table

hard ⇔ **soft**

Ground type	Type 1	Type 2	Type 3
Type 1 ground motion	0.30	0.35	0.40
Type 2 ground motion	0.80	0.70	0.60

Back data of 1996 version



Sand sampling

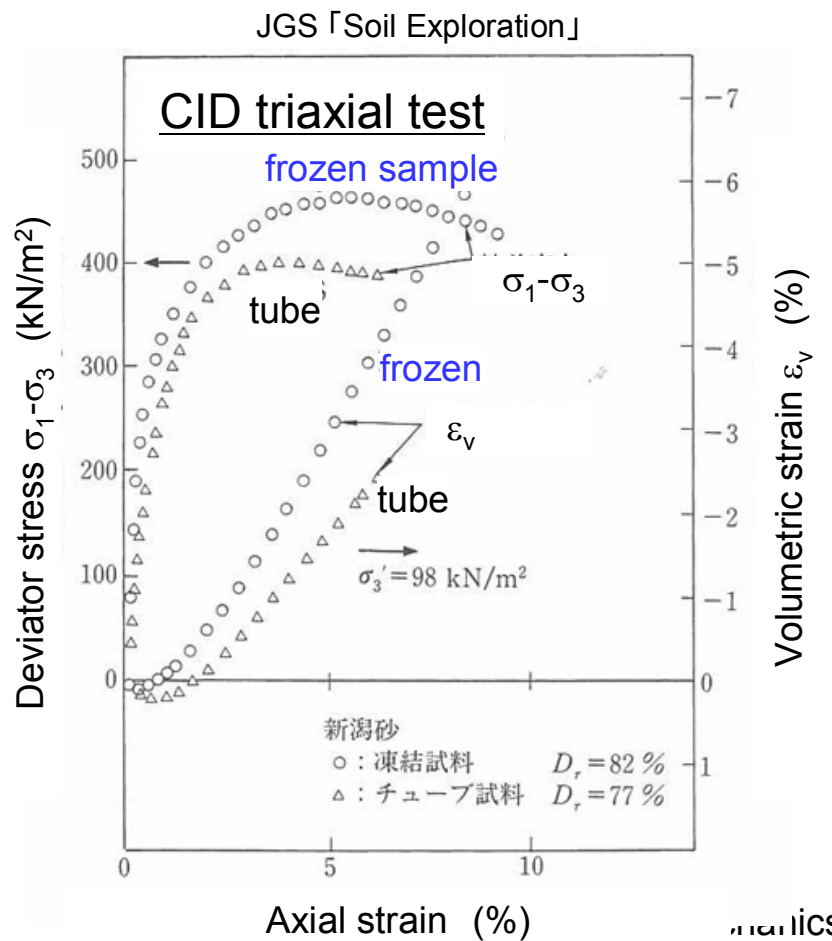
Method of sampler penetration:

Loose sand=> pushing

Hard, dense sand => rotary sampling

Mechanical properties of the sand sampled by these methods are different from those of ideal ones.

Properties of sand evaluated from sounding, field tests (e.g., SPT=>N-value)



To obtain the reliable properties

Freezing sampling
(凍結サンプリング)

